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n 型鉍-硒-碲及 p 型鉍-銻-碲熱電材料之製作與研究

Thermoelectric Properties of n-type  $\text{Cu}_{0.01}\text{Bi}_2\text{Se}_{0.3}\text{Te}_{2.7}$

and p-type  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ( $x=0.4-0.6$ )

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# 摘要

找尋新穎的熱電材料是現在許多物理、化學以及材料學家的熱門研究，熱電材料的益處在於可將生活中所產生的廢熱轉化成電能再度利用，可應用在於熱機或是冷凍機之上。

首先，在第一個研究之中，透過布理奇曼法在  $1050\text{ }^{\circ}\text{C}$  之下維持 10 個小時用以製作  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  塊材，以及透過水熱法製造出  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  奈米粒子，並且將兩種不同尺寸的粒子做不同比例的混合：奈米粒子(粒徑：20~100 奈米)重量百分比 0、10、20、30 和 100；接著探討火花電漿燒結法及奈米聚合物對熱電性質之影響。在實驗中發現材料中混入百分之三十的奈米粒子可提升熱電優質係數約一倍，由 0.35 提升至 0.74。若是可以將起初塊材的熱電優質係數提升至較良好的 0.7 以上，再透過奈米聚合和燒結，其熱電係數在 400 K 左右是可以超過 1 的。由這個研究顯示出：火花電漿燒結以及奈米聚合是可以有效的提升熱電優質係數，其主要原因來自於成功的降低熱傳導係數並同時維持住原本所擁有的電阻率以及席貝克係數的提升，而熱傳導降低因於樣品中的奈米結構所造成的粒子邊界增加、晶格的不匹配導致抑制聲子的傳熱所形成的結果。

第二個研究為一樣是透過布理奇曼法在  $750\text{ }^{\circ}\text{C}$  之下維持 12 個小時用以製作  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  塊材，其中  $x$  分別為 0.4、0.45、0.5 以及 0.6，本實驗主要為探討 Bi 的量對於  $\text{Bi}_x\text{Sb}_{1-x}\text{Te}_3$  所造成的影響。由結果中顯示  $x$  高於 0.5 和低於 0.5 所呈現的熱傳性質的趨勢有些許不同。在  $x$  為 0.45 的塊材中，得到本實驗中在室溫之下，最佳的熱電優質係數 1.5，獲得此結果的主要原因來自於相對較低的電阻率，並可觀察到  $x$  為 0.45 的載子濃度高於 0.4、0.5 和 0.6 的結果，其將可以佐證  $x=0.45$  塊材的低電阻率所造成的優質係數提升。

# Abstract

Physicists, chemists and material scientists at many major universities and research institutions throughout the world are attempting to create novel materials with high thermoelectric (TE) efficiency. It will be beneficial to harvest waste heat into electrical energy. Specialty heating and cooling are other major applications for this class of new TE materials.

In the first study, bulk and nanoparticles of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  were prepared separately. The  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  bulk was fabricated by Bridgeman method at 1050 °C for 10 hrs and the nanoparticles were made through hydrothermal method. Two kinds of powders were mixed with the ratios of NPs 0, 10, 20, 30 and 100 wt% and sintered by the SPS technique to form the composite specimens. The  $ZT$  value can be enhanced over 100% from 0.35 to 0.74 for specimen with 30 wt% nanoparticles. The consequence indicates that the SPS process and mixing nanocomposite can effectively enhance  $ZT$  value. The enhancements were caused mainly by the presence of nanostructured regions existing within the samples which lowered the thermal conductivity. The phenomenon is due to the presence of significant number of grain boundaries, shorten phonon mean free path and lattice mismatch.

For another investigation, the  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ingots with  $x=0.4, 0.45, 0.5$  and  $0.6$ . were fabricated by Bridgeman method at 750 °C for 12 hrs. We studied the effects of amount of Bi in  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  and the SPS process on the  $ZT$  enhancement. The experiment showed that for  $x > 0.5$ , the thermal property changed from a curve to a relatively linear line at the end. The best  $ZT$  is 1.5 ingot at 300 K for  $x=0.45$  specimen. The significant  $ZT$  improvement arises from the much-reduced electric resistivity. The lowest resistivity for  $x=0.45$  specimen is mainly due to the highest carrier concentration than those with  $x=0.4, 0.5$  and  $0.6$  ingots.

## 致謝

回首攻讀碩士班的這兩年，不論是在實驗以及做事情的方法上面都讓我學到很多，兩年過去了，當我認為已經開始對領域上有些概念和對儀器也開始熟悉的時候，就到了開始寫論文的時刻了。

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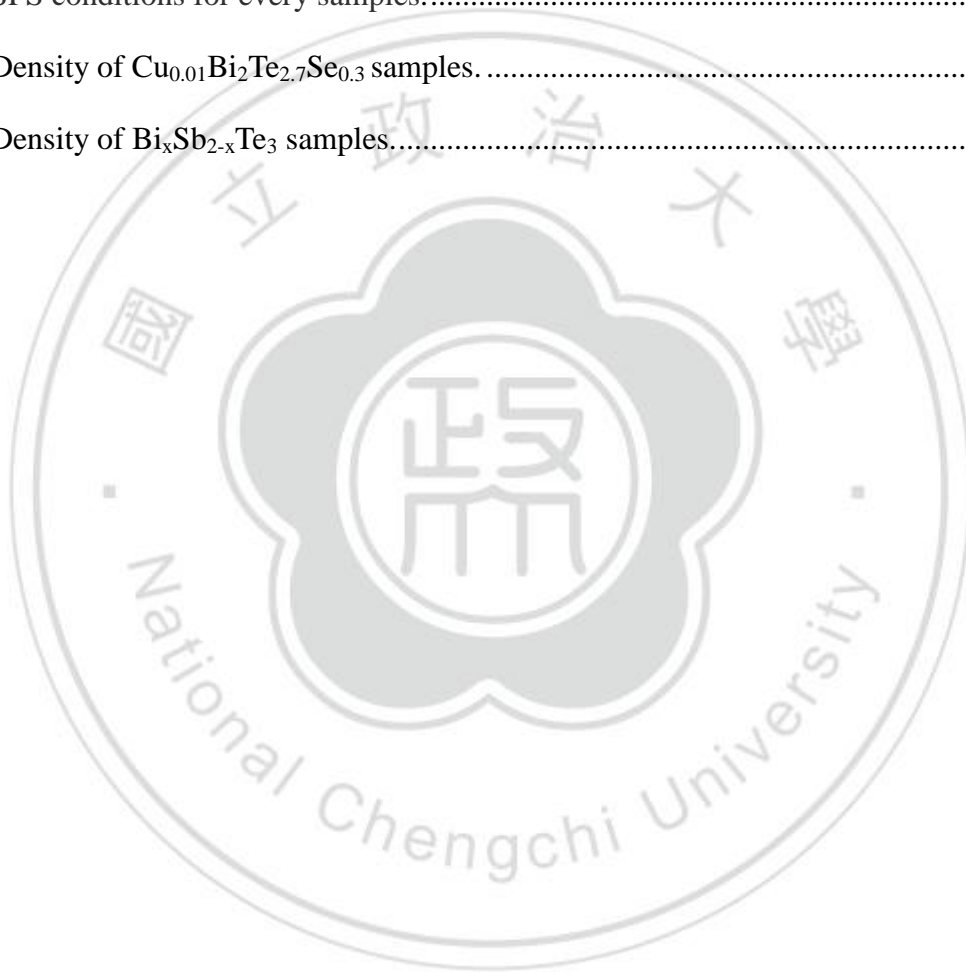


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# Chapter 1 Introduction

How to solve the energy crisis and environmental protection is a hot issue for scientists at present. It has several kinds of researches to focus on these issues. Firstly, the goal is to find the alternative energy sources which replace would the gasoline. The second, using some methods are place of nuclear power generator include solar, wind farm, hydroelectric, thermoelectric, etc.

Thermoelectric (TE) materials attract researchers' attentions not only due to their fundamental scientific interests, but also their potential applications in thermoelectricity. For decades, the region of thermoelectric materials research has focused on improving the efficiencies of the best thermoelectric material. An excellent review of traditional materials, such as  $\text{Bi}_2\text{Te}_3$  and  $\text{PbTe}$  with peak  $ZT$  value near 1 at different temperature ranges. In this study, the purpose is to find the high efficiency  $\text{Bi}_2\text{Te}_3$  based materials.

# 1.1 Thermoelectric Properties

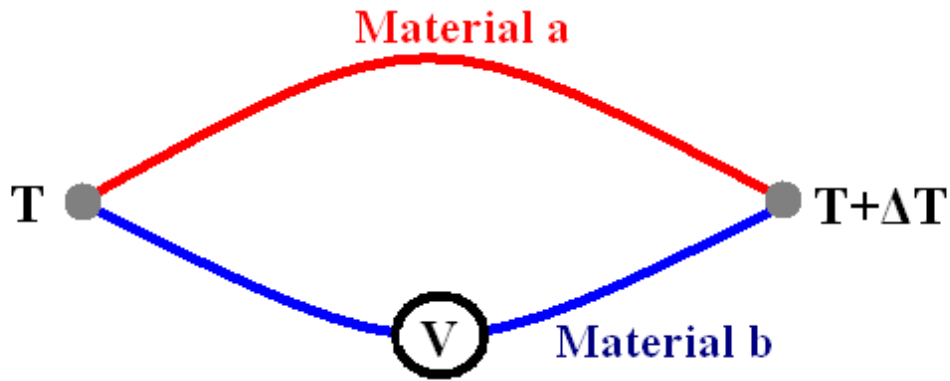
## 1.1.1 Seebeck Effect

In 1821, German-Estonian physicist *Thomas Johann Seebeck* found the effect which is the conversion of temperature differences directly into electricity called Seebeck effect.

The Seebeck effect, or Seebeck coefficient,  $S$ , describes the establishment of a voltage gradient across a material in response to a temperature gradient (Fig.1.1):

$$S_{ab} = \frac{dV}{dT} \left( \frac{V}{K} \right) \quad (1.1)$$

where  $S_{ab}$  is the relative thermopower across the junction of two materials. Intuitively, the establishment of a temperature gradient implies a higher concentration of charge carriers at the cold end of the sample, which in turn corresponds to the establishment of a voltage differential across the sample. As a corollary, the sign of the Seebeck coefficient is typically negative for n-type electrical conduction, where electrons are the primary charge carriers, and positive for p-type conduction, where holes are the majority carriers.



$$\Delta V = S \Delta T$$

Fig. 1.1 The Seebeck effect occurs between the junction of two dissimilar materials when a temperature gradient is present

### 1.1.2 Peltier Effect

In 1834, French physicist *Jean Charles Athanase Peltier* found that the junctions of dissimilar metals were heated or cooled, depending upon the direction in which an electrical current passed through them. Heat generated by current flowing in one direction was absorbed if the current was reversed. The Peltier effect is found to be proportional to the first power of the current, not to its square, as is the irreversible generation of heat caused by resistance throughout the circuit. The junction emf,  $\pi_{ab}$ , is known as the Peltier coefficient, is expressed as:

$$\Pi_{AB} = -\Pi_{BA} = \frac{1}{I} \frac{dQ}{dt} \quad (1.2)$$

where  $dQ/dt$  is the rate of heat transfer at the junction, and  $I$  is the electrical current.

$\Pi_{AB}$  means the current from A to B and  $\Pi_{BA}$  inverse to  $\Pi_{AB}$ . The Peltier effect usually applied in the thermoelectric refrigerator.

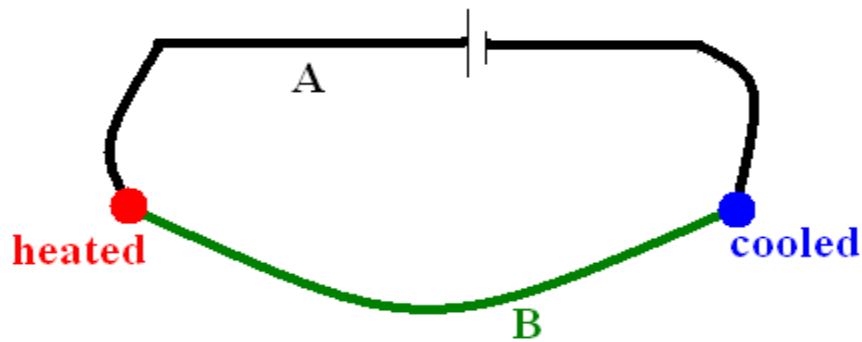


Fig. 1.2 The Peltier effect. When an electrical current is injected, heat is expelled or absorbed at the junction between material A and B.

### 1.1.3 Thomson Effect

When a current flows through an unequally heated metal, there is an absorption or evolution of heat in the body of the metal that is Thomson effect.

The metals which show positive Thomson's effect are Cu, Sn, Ag, Cd, Zn... etc, it is found that hot end is at high potential and cold end is at low potential. Heat is evolved when current is passed from hotter end to the colder end and heat is absorbed when current is passed from colder end to hotter end.



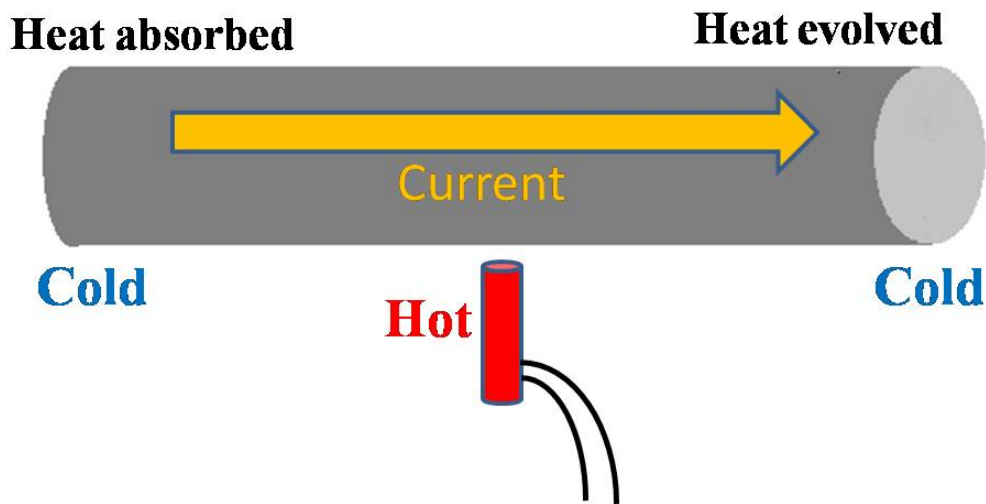


Fig. 1.3 Diagram of positive Thomson's effect.

In the other case that the hot end is at low potential and the cold end is at higher potential. Heat is evolved when current is passed from colder end to the hotter end and heat is absorbed when current flows from hotter end to colder end that called negative Thomson effect with the metals which are Fe, Co, Bi, Pt, Hg... etc

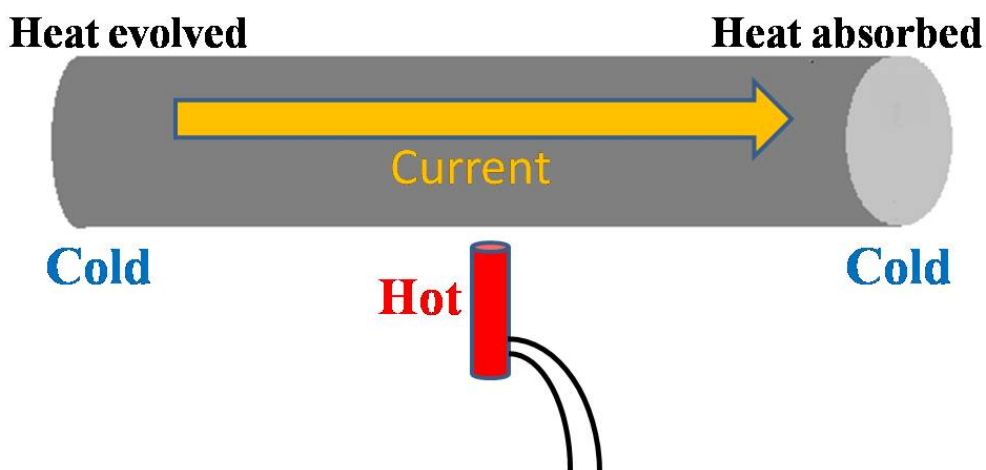


Fig. 1.4 Diagram of negative Thomson effect.

The Thomson effect states that in the absence of Joule heating, the heat gained or

lost is given by

$$\frac{dQ}{ds} = \tau I \frac{dT}{ds} \quad (1.3)$$

where  $s$  is a spatial coordinate,  $I$  is the electrical current,  $T$  is the temperature,  $Q$  is the heat, and  $\tau$  is the Thomson coefficient. It should be noted that while the Seebeck and Peltier coefficients describe heat transfer in a system of two materials, the Thomson effect describes heat flow in a single material. From the Thomson effect, it can be shown that

$$\tau_a - \tau_b = T \frac{dS_{ab}}{dT} \quad (1.4)$$

and consequently that

$$\Pi_{ab} = S_{ab}T \quad (1.5)$$

### 1.1.4 The Figure of Merit

The efficiency of power generation modules is described in terms of the efficiency of a heat engines, on the other hand the coefficient of performance (C.O.P.) is characterized for the efficiency of refrigeration modules. In similar case, it is possible to relate the expressions describing the efficiency to a parameter that contains the relevant thermal, electrical, and thermoelectric parameters, the tuning of which is at the center of research into thermoelectric materials. The relation of this parameter, the “Figure of Merit” to the coefficient of performance and heat engine efficiency is outlined here.

$$\text{Figure of Merit (Z)} = \frac{S^2}{\kappa\rho} \quad (1.6)$$

Apply a temperature differential to a bulk material and the electrons get the

energy from the hot side to cold side arrived to balance (Fig.1.5).

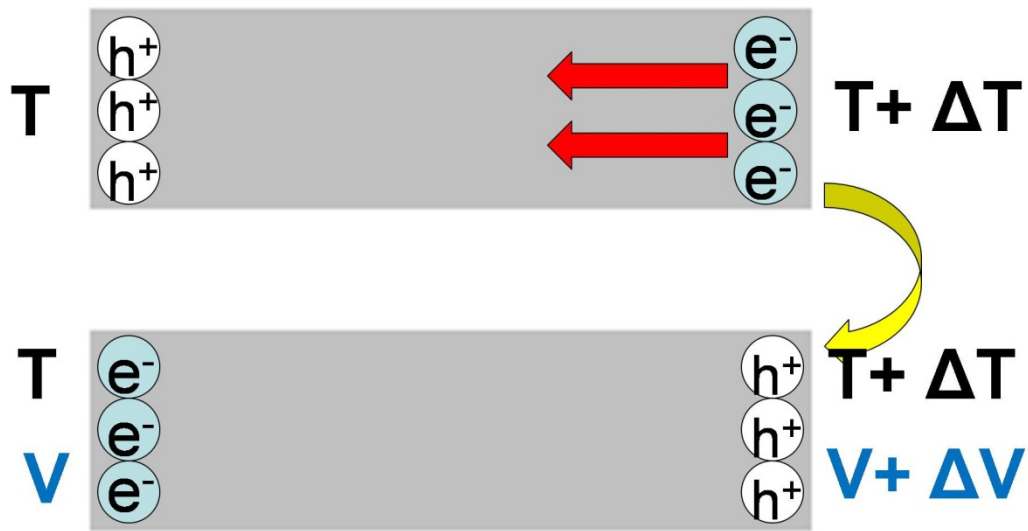


Fig. 1.5 Diagram of the temperature difference balance against voltage difference

The bulk similar to a system compose between a electric resistance and thermal resistance (Fig. 1.6)

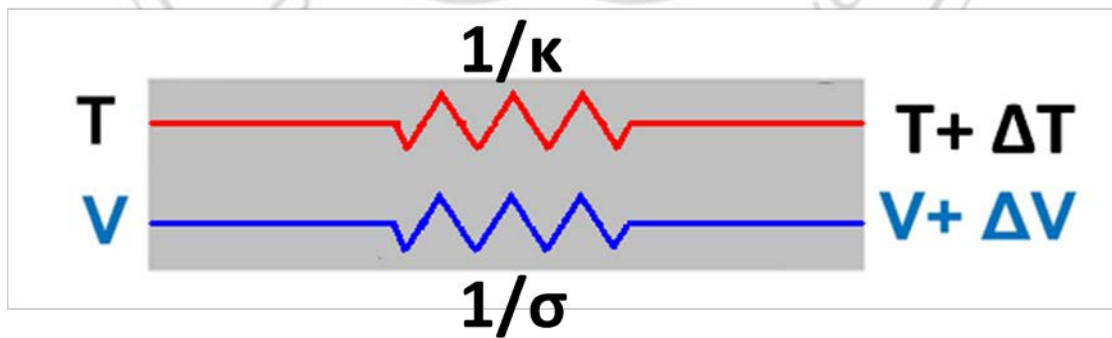


Fig. 1.6 Diagram of electrical circuit

The coefficient of performance,  $\Phi$ , is related to the total heat flow,  $dQ/dt$ , and the power input,  $P$ , as follows:

$$\Phi = \frac{1}{P} \frac{dQ}{dt} \quad 1.7)$$

Here,  $Q$  is the sum of heat flow due to the thermal conductance of the material,  $Q_K$ , the Peltier heat flow,  $Q_{II}$ , and the heat loss due to Joule heating,  $Q_I$ . That is,

$$Q = Q_K + Q_{II} + Q_I \text{ where, } K \text{ is thermal conductance}$$

$$Q_K = -K\Delta T \quad (1.8)$$

$$Q_{II} = IST \quad (1.9)$$

$$Q_I = -\sigma(\Delta V)^2 \quad (1.10)$$

The power supplied to the device is giving by Joule expression:

$$P = I^2R \quad (1.11)$$

Therefore the C.O.P. becomes

$$\Phi = \frac{Q}{P} = \frac{-K\Delta T + IST - \sigma(\Delta V)^2}{I^2R} \quad (1.12)$$

By differential calculation  $d\Phi/dt = 0$  can get the maxima value of  $I$

$$I_{Max} = \frac{K\Delta T + \sigma(\Delta V)^2}{ST} = \frac{2K\Delta T}{ST} \quad (1.13)$$

Cause balance between thermal and electrical. Then, replace  $I_{Max}$  back into equation

(1.12) and simpler the formula

$$\Phi_{Max}(I_{Max}) = \frac{\frac{S^2T^2}{RK} - 4\Delta T}{4\Delta T} \quad (1.14)$$

In equation (1.14) thermal conductance  $K$  and resistance  $R$  depend on dimensions of sample. Hence, using the thermal conductivity  $\kappa$  and the electrical resistivity  $\rho$  to substitute for its.

It is customary to define a new quantity, the figure of merit,  $Z$ , as

$$Z = \frac{S^2}{\kappa\rho} \quad (1.15)$$

The dimension of  $Z$  is  $T^{-1}$ , hence, let this value multiply to  $T$  defined the new coefficient  $ZT$  that becomes dimensionless shown as.

$$ZT = \frac{S^2 T}{\kappa \rho} = \frac{S^2 \sigma T}{\kappa} \quad (1.16)$$

Thus the C.O.P. becomes

$$\Phi_{\text{Max}} = \frac{ZT^2 - 4\Delta T}{4\Delta T} \quad (1.17)$$

The efficiency of a heat engine is given by the well-known formula:

$$\eta = \frac{W}{dQ/dt} \text{ where,}$$

$$W = I\Delta V_{\text{Seebeck}} - I\Delta V_R = IS\Delta T - \sigma(\Delta V)^2 \quad (1.18)$$

$$Q = \kappa\Delta T + IST - \sigma(\Delta V)^2 \quad (1.19)$$

Then the transformational efficiency of electrical energy as:

$$\eta = \frac{IS\Delta T - \sigma(\Delta V)^2}{\kappa\Delta T + IST - \sigma(\Delta V)^2} \quad (1.20)$$

It also has the maxima  $\eta$  value with  $I_{\text{Max}}$  through derivative of  $\eta$  equal to zero. After some simplification, that is

$$I_{\text{Max}} = \frac{S\Delta T}{\rho \sqrt{1 + \left(\frac{S^2}{\rho\kappa}\right)T + 1}} = \frac{S\Delta T}{\rho \sqrt{1 + (ZT)T + 1}} \quad (1.21)$$

Replace  $I_{\text{Max}}$  into eq. [1.20] and simplify it that is reducing to

$$\eta = \frac{T_H - T_C}{T_H} \frac{\sqrt{1 - ZT} - 1}{\sqrt{1 + ZT} + \frac{T_C}{T_H}}, \text{ where } T = \frac{T_H + T_C}{2} \quad (1.22)$$

When  $Z \rightarrow \infty$ , the expression for the efficiency given in eq. (1.22) approaches the Carnot limit. The calculations showing the relationship of theoretical  $ZT$  values to the relative Carnot efficiency and the C.O.P. have revealed an interesting trend.[2]

It was shown that a  $ZT$  in the range of 2-3 corresponds to a Carnot efficiency of about 40-50% in the power generation scheme or a C.O.P. of 2-3 in the refrigeration configuration.[1]

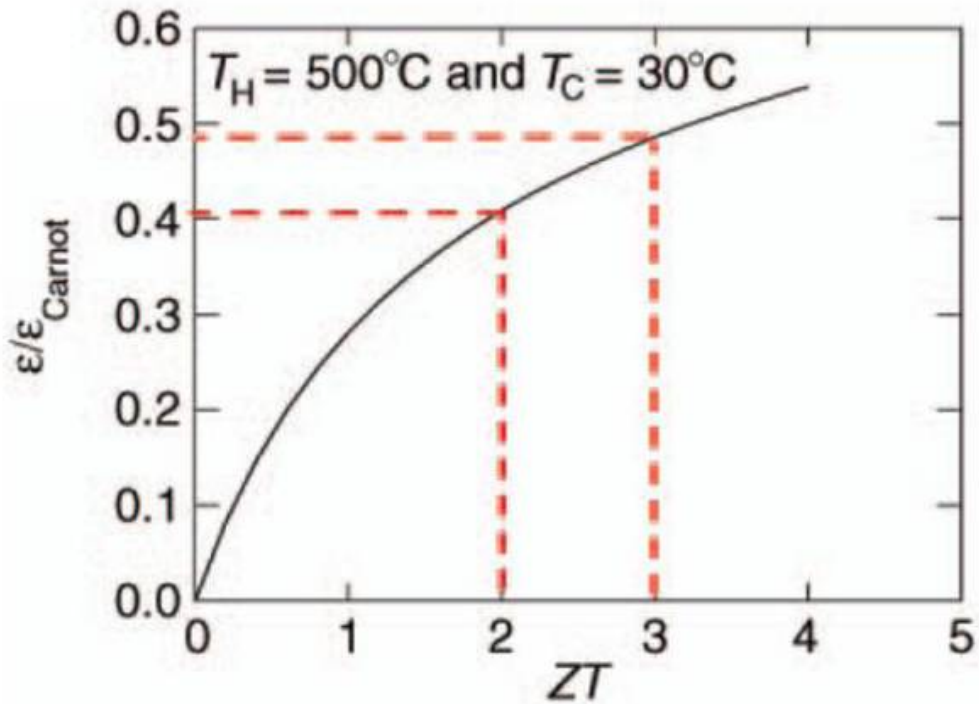


Fig. 1.7 Figure of merit,  $ZT$ , as a function of relative Carnot efficiency. [2].

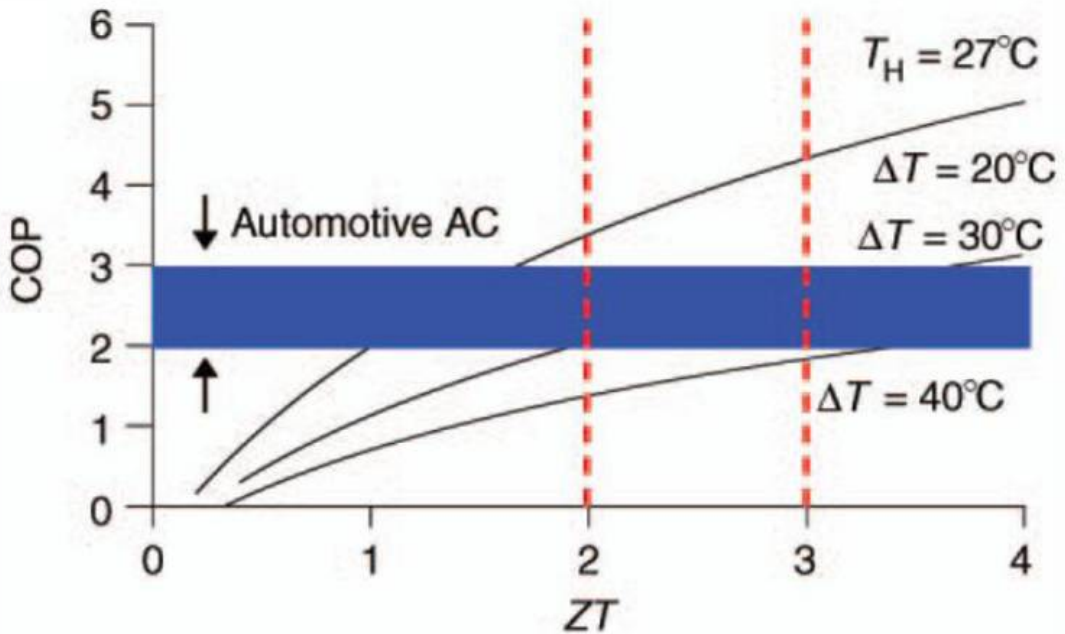


Fig. 1.8  $ZT$  is a function of coefficient of performance at various temperatures. [2].



## 1.2 Crystal Growth Methods

### 1.2.1 Bridgman–Stockbarger Method

The methods named by Harvard physicist Percy Williams Bridgman and MIT physicist Donald C involve heating polycrystalline material above its melting point and slowly cooling it from one end of its container, where a seed crystal is located. The process can be carried out in a horizontal or vertical geometry. The difference between the Bridgman technique and Stockbarger technique is subtle: while a temperature gradient is already in place for the Bridgman technique, the Stockbarger technique requires pulling the boat through a temperature gradient to grow the desired single crystal.

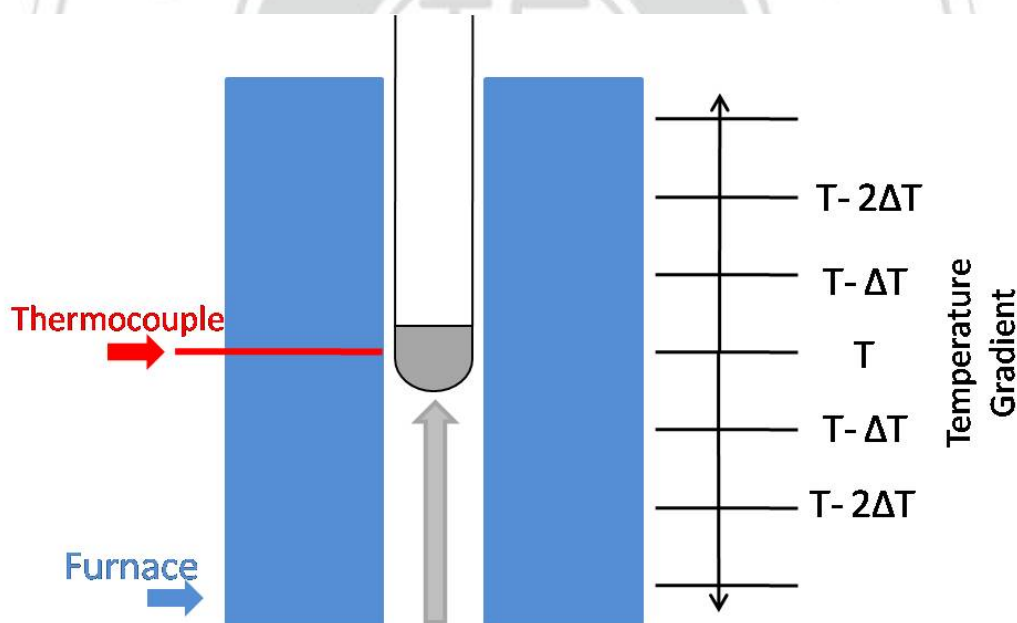


Fig. 1.9 Diagram of Bridgman method for crystal growth

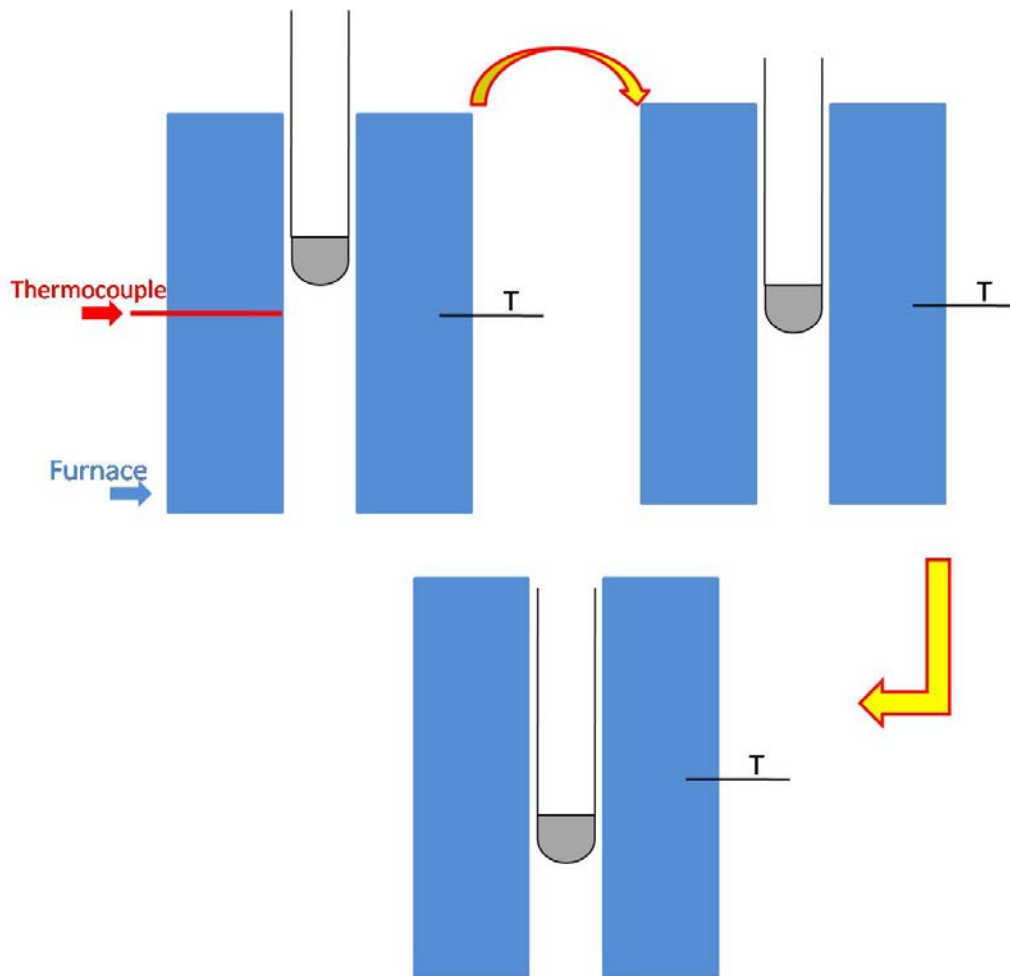


Fig.1.10 Diagram of Stockbarger technique for crystal growth

## 1.2.2 Powder Metallurgy Method

The powder metallurgy process generally consists of four basic steps:

- (1) Powder manufacture
- (2) Powder blending
- (3) Compacting
- (4) Sintering or Annealing

The powder metallurgy existed in Egypt as early as 3000 B.C. It can improve the compaction and the material properties through the sintering process. The technical

and commercial advantages of producing parts from powder can be summarized as below:

Production to near net shape

Few or no secondary operations

High material utilization from low levels of 'in process scrap'

Homogeneous powder and hence part, chemical composition due to absence of gross solidification segregation and uniform pre-alloyed powder particle composition

Unique compositions and structures possible as there is no melting

Non-equilibrium compositions possible

Metallurgical structures are usually fine and isotropic [5]

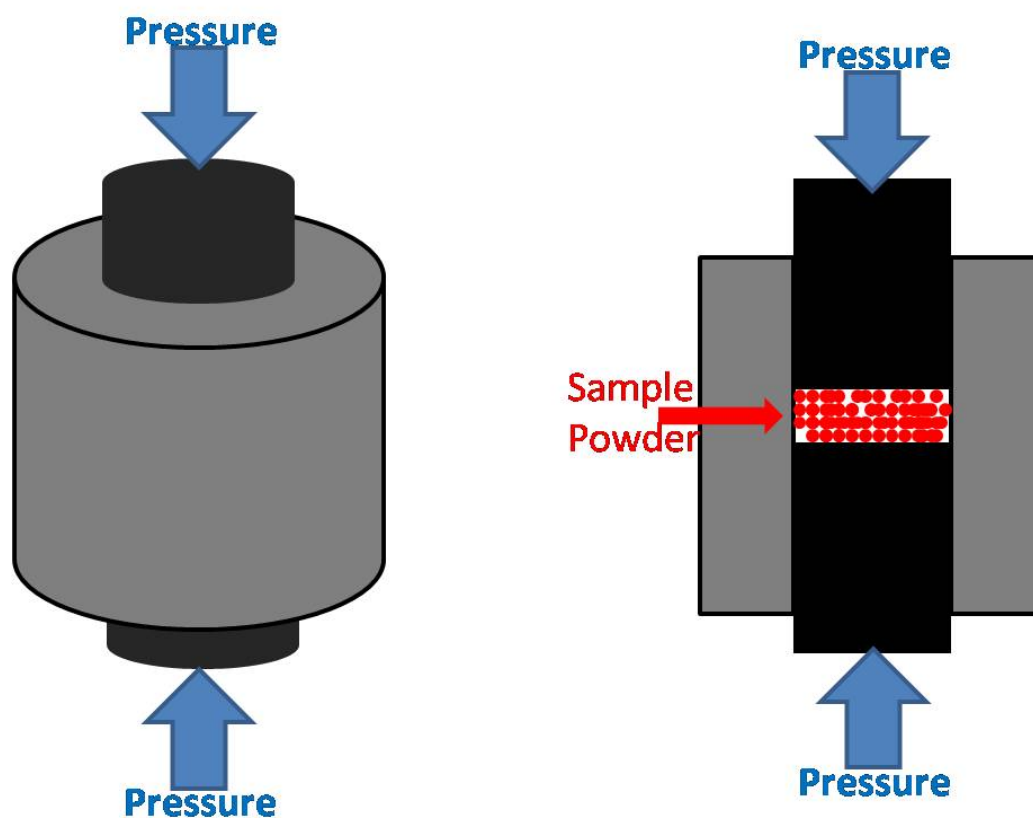


Fig. 1.11 Diagram of the compacted process of powder metallurgy method

### 1.3 Nomenclature

<b>Symbol</b>	<b>Units</b>	<b>Description</b>
<b>A</b>	<b>m<sup>2</sup></b>	<b>Area</b>
<b>L</b>	<b>m</b>	<b>Length</b>
<b>R</b>	<b>Ohm(<math>\Omega</math>)</b>	<b>Resistance</b>
<b><math>\rho</math></b>	<b><math>\mu\text{Ohm}\cdot\text{m}(\mu\Omega\cdot\text{m})</math></b>	<b>Resistivity</b>
<b>S</b>	$\frac{\mu\text{V}}{\text{K}}$	<b>Seebeck coefficient</b>
<b>D</b>	$\frac{\text{mm}^2}{\text{s}}$	<b>Thermal diffusivity</b>
<b>d</b>	$\frac{\text{g}}{\text{cm}^3}$	<b>Density</b>
<b><math>\kappa</math></b>	$\frac{\text{W}}{\text{mK}}$	<b>Thermal Conductivity</b>
<b>T</b>	<b>K</b>	<b>Temperature</b>
<b>Z</b>	<b>K<sup>-1</sup></b>	<b>Figure of Merit</b>

# Chapter 2 Experimental Techniques

## 2.1 Equipments

The equipment used in this investigation is listed in Table 2.1.

Table 2.1 Equipments used in this investigation.

Type	Manufacturer / Model	Specifications
X-ray Diffraction	PANalytical/ X'pert Powder	2 $\theta$ : 10° ~100° Powder / Bulk
Thermal Properties Measure System	NETZSCH/LFA-457	Thermal Diffusivity -125~500°C
Thermal Properties Measure System	TA/DSC-Q100	Heat Capacity -180~400°C
Electrical Properties Measure System	ULVAC/ZEM-3	Seebeck coefficient and resistivity R.T. ~ 800°C
Sintering System	ULVAC/SPS-515S	30~90Mpa Max. heating rate 1000°C/min

## 2.2 Bulk Fabrication

Prepare the powder with the correct ratio (table 2.2, 2.3) in dry box and put into the smaller tube (10 x 12 x 60 mm) after blending, then sealed in the bigger quartz tube (13 x 16 x 20 mm) under the pressure below  $10^{-5}$  torr (Fig. 2.1). Put the quartz tube with the sample powder into furnace to fabricate (Fig. 2.2) with the annealing pattern (Fig. 2.3, 2.4).

Table 2.2 Weighed of each powder for  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  fabrication

<b><math>\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}</math></b>			
	<b>Weight (g)</b>	<b>Weight %</b>	<b>Atomic %</b>
<b>Cu Powder</b>	<b>0.052</b>	<b>1</b>	<b>--</b>
<b><math>\text{Bi}_2\text{Te}_3</math></b>	<b>4.8046</b>	<b>100</b>	<b>90</b>
<b>Bi Powder</b>	<b>0.2508</b>		<b>4</b>
<b>Se Powder</b>	<b>0.1421</b>		<b>6</b>
<b>Te 3%</b>	<b>0.1559</b>	<b>3</b>	<b>--</b>



Table 2.3 Weighed of each powder for  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ( $x=0.4, 0.45, 0.5$  and  $0.6$ )  
fabrication

<b><math>\text{Bi}_{0.4}\text{Sb}_{1.6}\text{Te}_3</math></b>			
	<b>Weight (g)</b>	<b>Weight %</b>	<b>Atomic %</b>
<b><math>\text{Bi}_2\text{Te}_3</math></b>	<b>1.1647</b>	<b>100</b>	<b>20</b>
<b><math>\text{Sb}_2\text{Te}_3</math></b>	<b>3.6439</b>		<b>80</b>
<b>Te 3%</b>	<b>0.1443</b>	<b>3</b>	<b>--</b>
<b><math>\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3</math></b>			
	<b>Weight (g)</b>	<b>Weight %</b>	<b>Atomic %</b>
<b><math>\text{Bi}_2\text{Te}_3</math></b>	<b>1.2425</b>	<b>100</b>	<b>22.5</b>
<b><math>\text{Sb}_2\text{Te}_3</math></b>	<b>3.3481</b>		<b>77.5</b>
<b>Te 3%</b>	<b>0.1376</b>	<b>3</b>	<b>--</b>
<b><math>\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3</math></b>			
	<b>Weight (g)</b>	<b>Weight %</b>	<b>Atomic %</b>
<b><math>\text{Bi}_2\text{Te}_3</math></b>	<b>1.922</b>	<b>100</b>	<b>25</b>
<b><math>\text{Sb}_2\text{Te}_3</math></b>	<b>4.771</b>		<b>75</b>
<b>Te 3%</b>	<b>0.208</b>	<b>3</b>	<b>--</b>
<b><math>\text{Bi}_{0.6}\text{Sb}_{1.4}\text{Te}_3</math></b>			
	<b>Weight (g)</b>	<b>Weight %</b>	<b>Atomic %</b>
<b><math>\text{Bi}_2\text{Te}_3</math></b>	<b>1.6566</b>	<b>100</b>	<b>30</b>
<b><math>\text{Sb}_2\text{Te}_3</math></b>	<b>3.0234</b>		<b>70</b>
<b>Te 3%</b>	<b>0.1414</b>	<b>3</b>	<b>--</b>

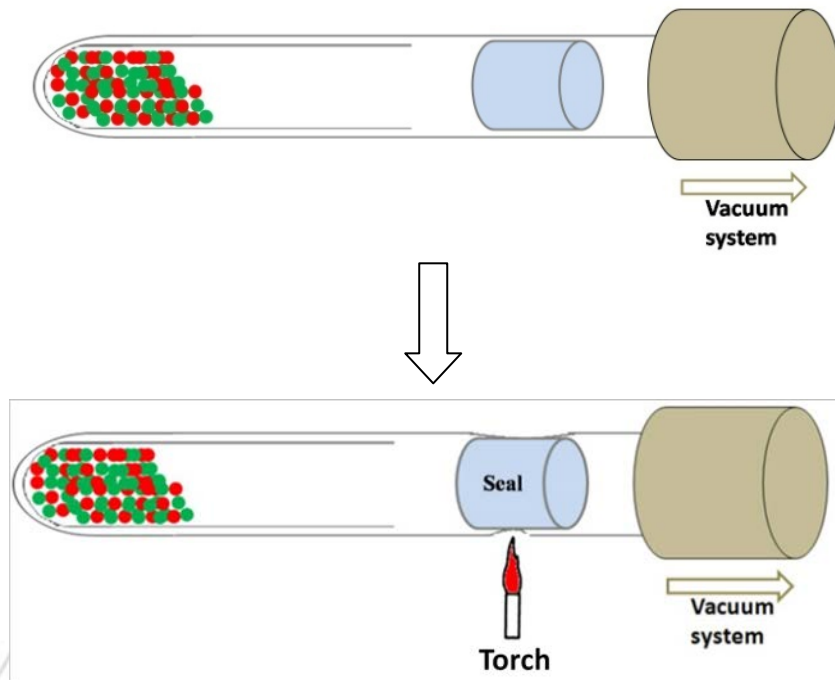


Fig.2.1 Diagram of quartz tube sealing

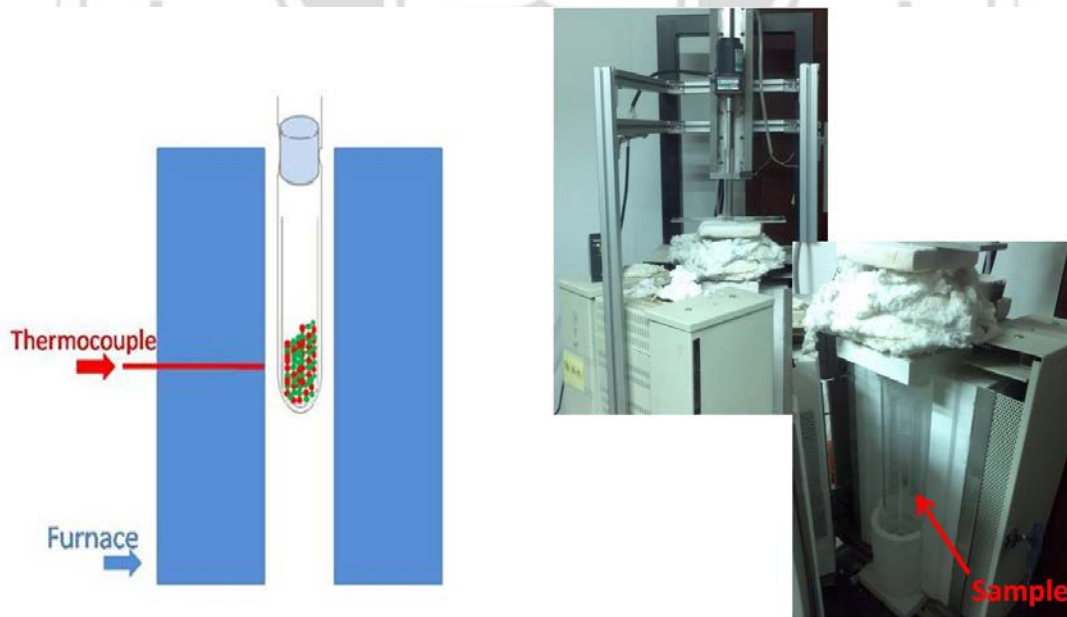


Fig. 2.2 Left: diagram of sample melting in furnace; Right: real photo.

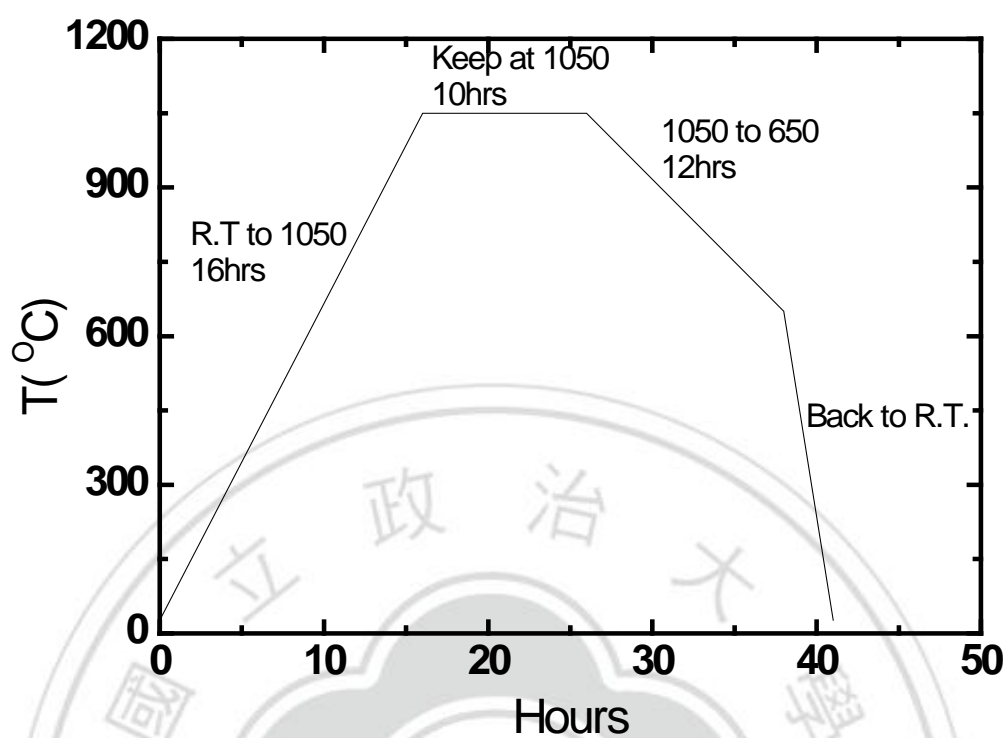


Fig. 2.3 Anneal pattern for  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$

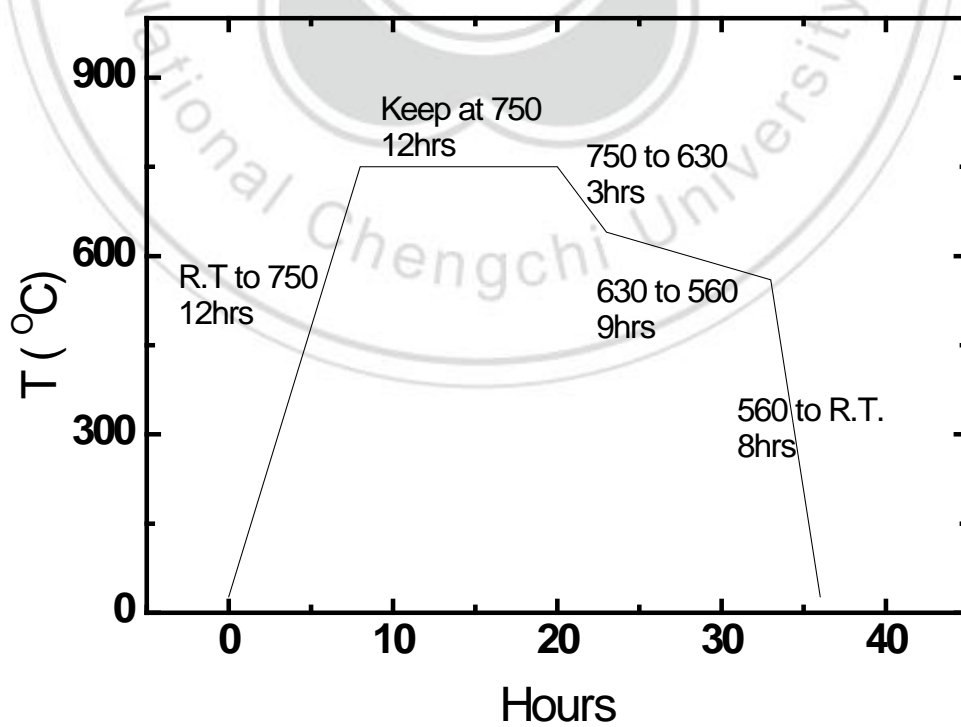


Fig. 2.4 Anneal pattern for  $\text{Bi}_x\text{Sb}_{1-x}\text{Te}_3$  ( $x=0.4, 0.45, 0.5$  and  $0.6$ )

## 2.3 X-ray Diffraction

X-ray diffraction (XRD) is a universal method to analysis about the chemical composition and crystallographic structure of natural and manufactured materials. After the bulk fabrication, confirming the phase structure by it.

According to the Bragg's law (Fig.2.5):

$$2d\sin\theta = n\lambda \quad (2.1)$$

where,  $d$  is the distance between two nearest layers of atoms,  $\lambda$  is the wavelength of indicated light and  $\theta$  is the angle between indicated light and layer.

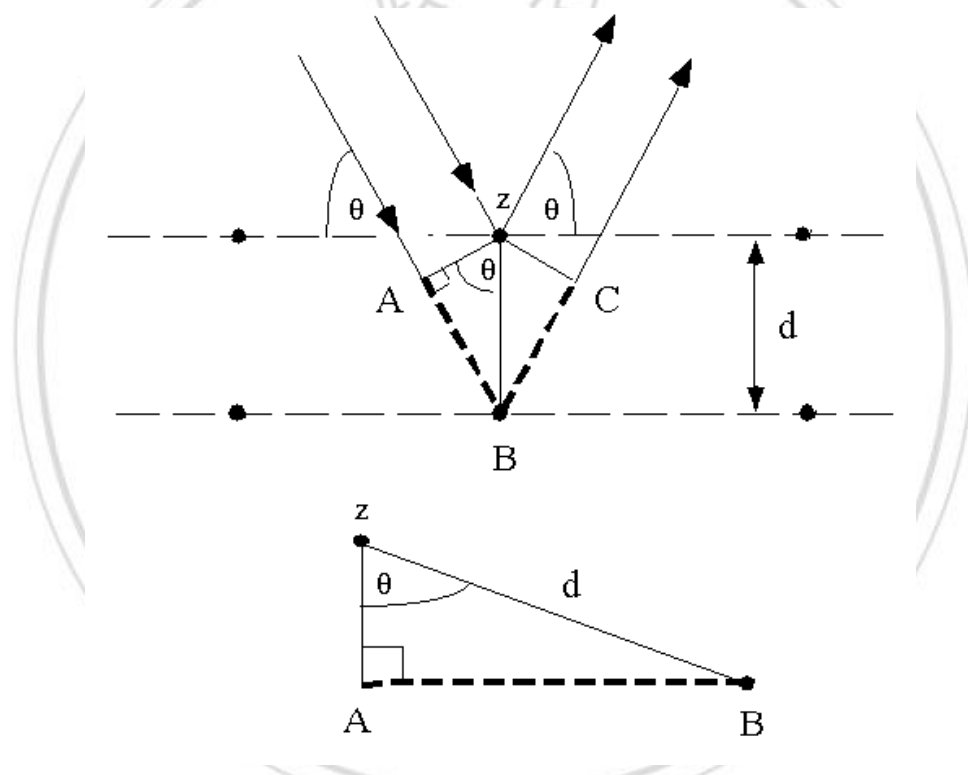


Fig.2.5 Bragg's diffraction

Although Bragg's law was used to explain the interference pattern of X-rays scattered by crystals, diffraction has been developed to study the structure of all states of matter with any beam, e.g., ions, electrons, neutrons, and protons, with a wavelength similar to the distance between the atomic or molecular structures of interest.

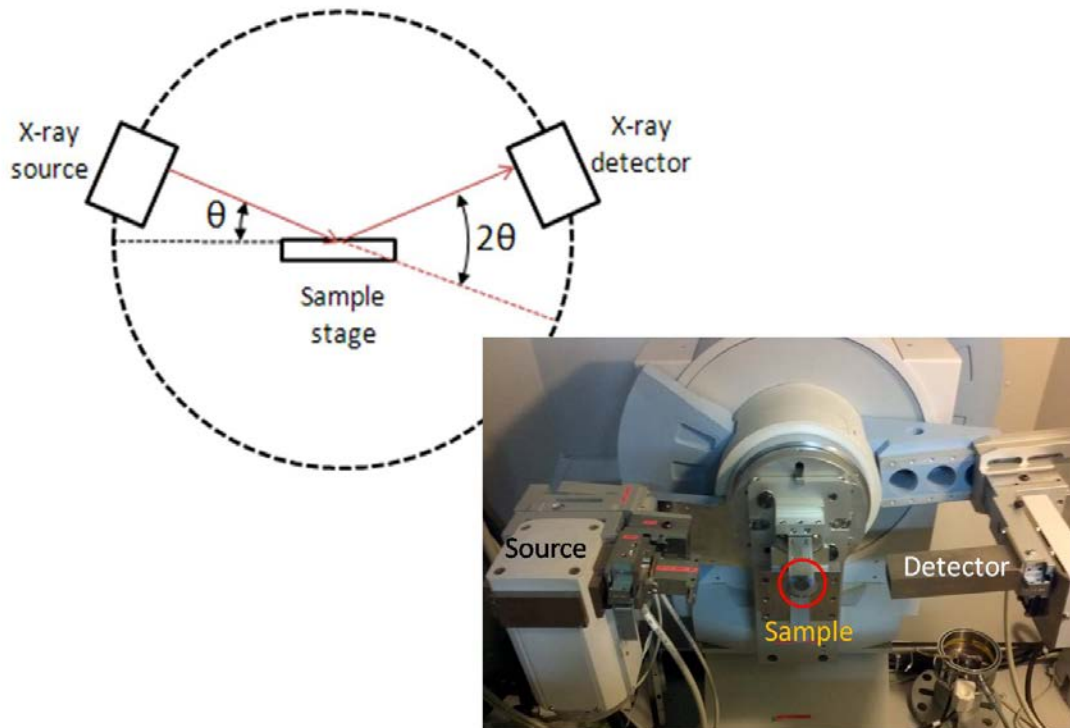


Fig.2.6 measured parts of XRD, left: diagram; right: real photo

When indicated X-ray's optical path difference satisfied with Bragg's law that reflected light generate the constructive interference. Take the signals compared to reference from the database to confirm the phase structure.

## 2.4 Thermal Properties Measure Systems

### 2.4.1 LFA 457– Thermal Diffusivity

The front side of a plane parallel solid sample is heated by a short laser pulse. The heat induced propagates through the sample and causes a temperature increase on the rear surface. This temperature rise is measured versus time using an infrared detector. The thermal diffusivity,  $D$ , and in many cases also the specific heat,  $C_p$ , can

be ascertained using the measured signal. If the density,  $d$ , is known, the thermal conductivity,  $\kappa$ , can be determined

$$\kappa(T) = D(T)C_p(T)d(T) \quad (2.2)$$

The Sample is prepared with thickness  $t$ , then thermal diffusivity,  $D$ , can be measured by LFA457 follow the formula:

$$D = 0.1388 \frac{t^2}{\tau_{0.5}} \quad (2.3)$$

where,  $\tau_{0.5}$  is the half-time of IR-detector detect the signal from minima to maxima.

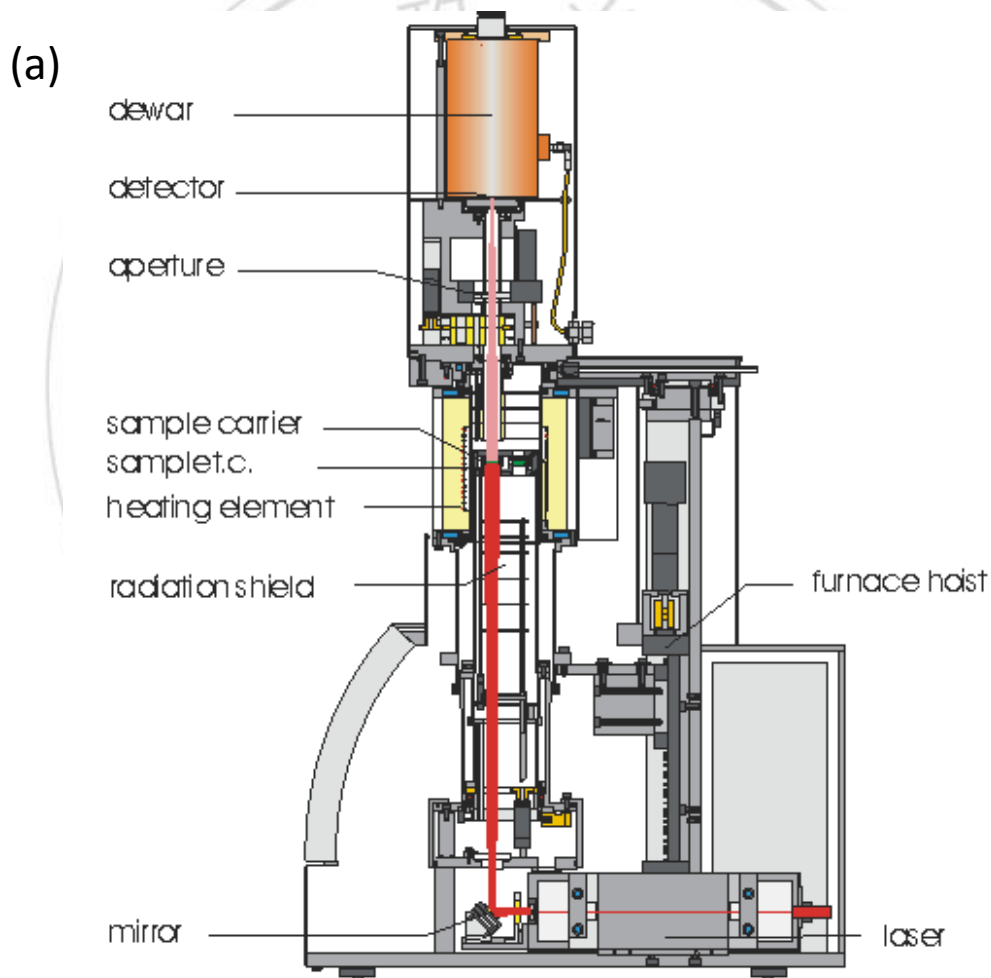


Fig. 2.7 Diagram of laser excited in LFA



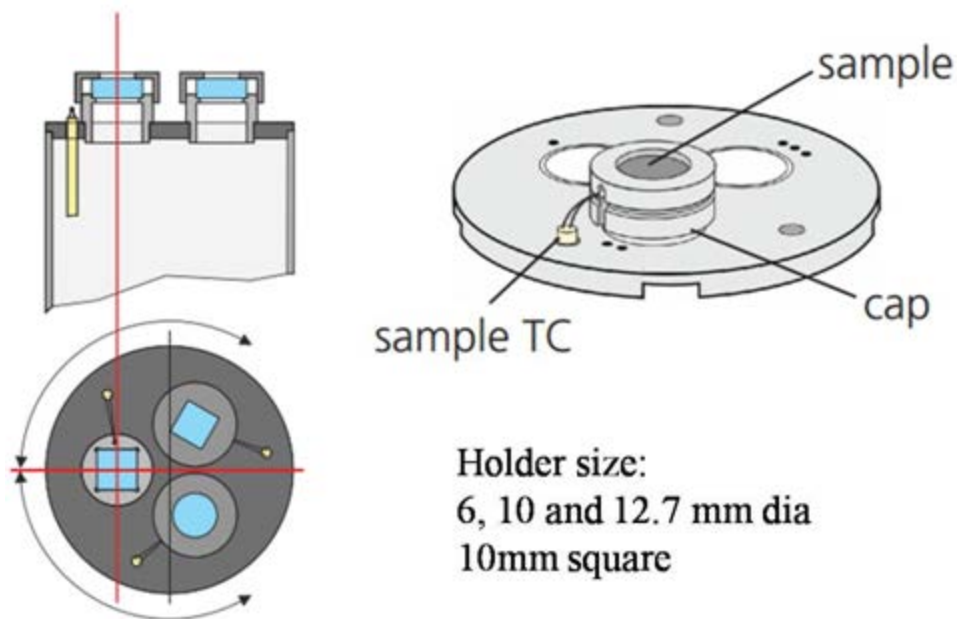


Fig. 2.8 Diagram of LFA's holder

## 2.4.2 DSC Q100 – Specific Heat

Differential Scanning Calorimeters (DSC) measures temperatures and heat flows associated with thermal transitions in a material. Common usage includes investigation, selection, comparison and end-use performance evaluation of materials in research, quality control and production applications. Properties measured by TA Instruments' DSC techniques include glass transitions, “cold” crystallization, phase changes, melting, crystallization, product stability, cure kinetics, and oxidative stability. In this study, prepare the sample which is already measure the weight, next seal in the Aluminum dish (Fig.2.9).

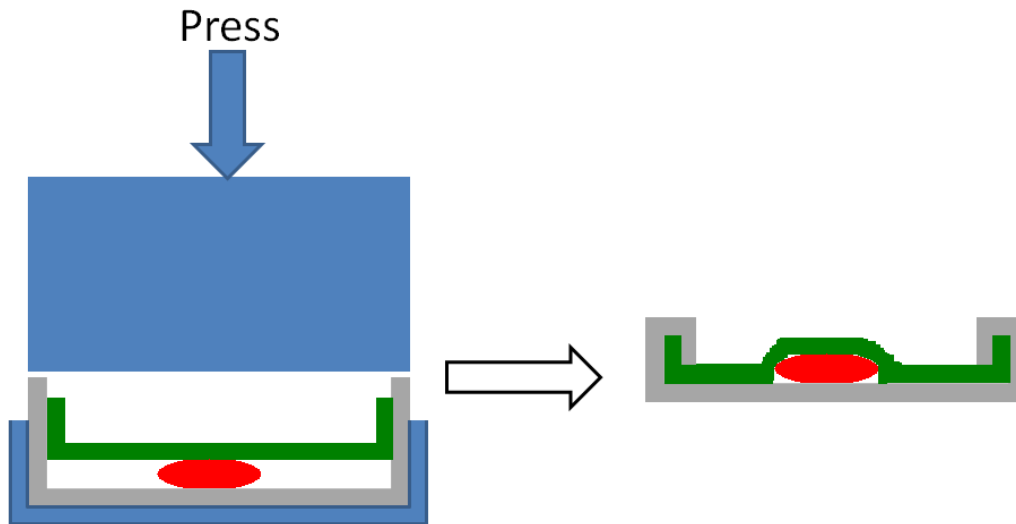


Fig. 2.9 Diagram of sealing sample in the aluminum dish

then, put the sample which is already sealing into the DSC chamber to measure specific heat by heat flow between reference platform and sample platform, according to:

$$\Delta H = mC_p\Delta T \quad (2.4)$$

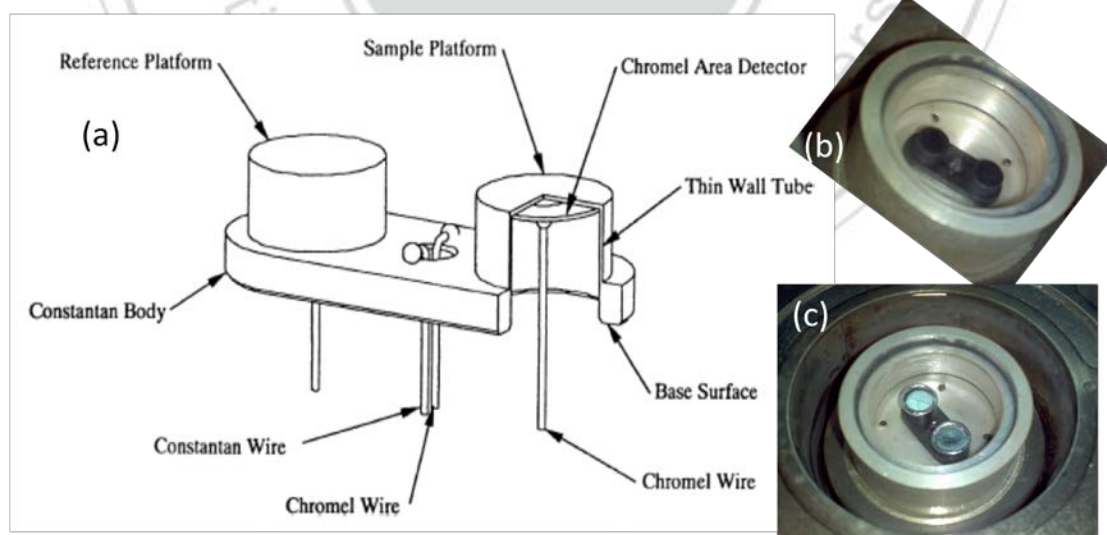


Fig.2.10 The tools in the DSC chamber, a) diagram of measured parts; b) real photo; c) real photo with reference (up) and sample (down).

### 2.4.3 Density

According to the Archimedes principle which is shown any floating object displaces its own weight of fluid; any object, wholly or partially immersed in a fluid, is buoyed up by a force equal to the weight of the fluid displaced by the object.

$$F = \text{Volume of sample} \times \text{density of fluid}$$

Therefore, the density of sample can measure by it.

Take a beaker which has about 15cc DI water inside putting on the balance and zero it. Next, prepare an aluminum wire (10 cm length, 25  $\mu\text{m}$  dia. ) connect to the sample with GE varnish (Fig.2.11L), then, hand the a part of wire let the sample sink in water and read the balance value which is the volume of sample (Fig.2.11R).

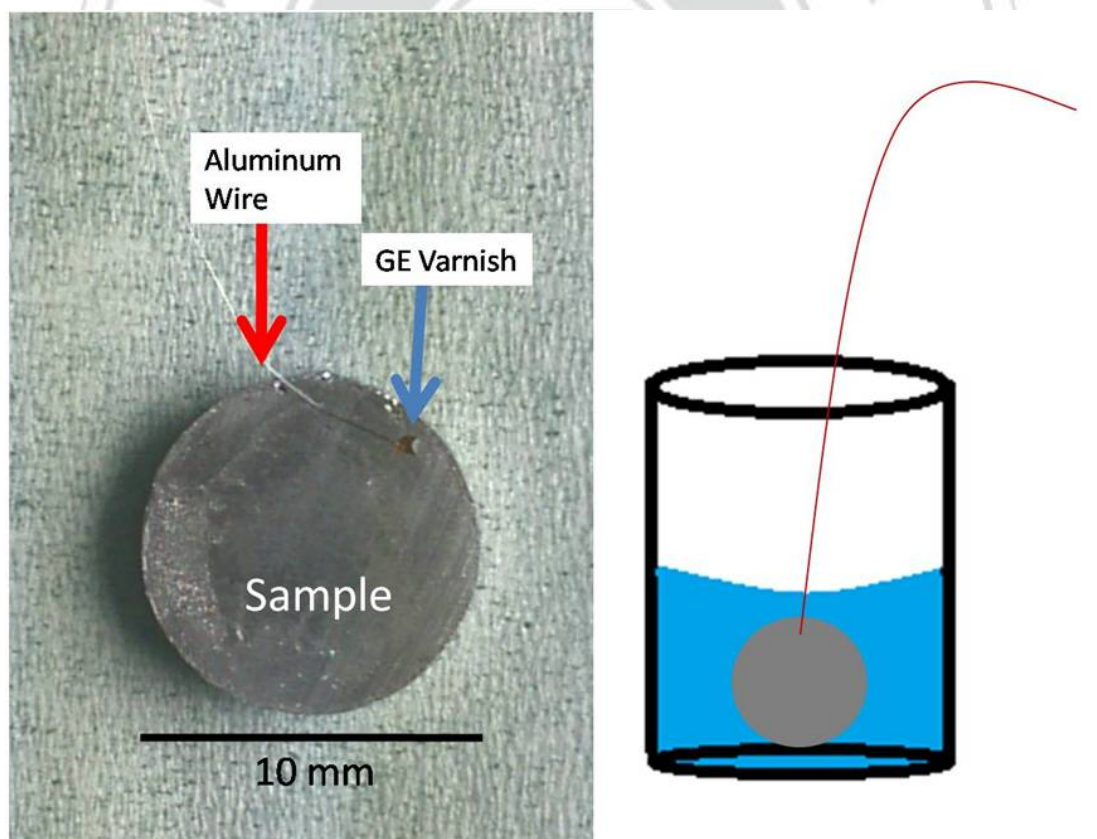


Fig. 2.11 Left: photo of connect the sample with GE varnish;

Right:Diagram of density measurement

## 2.5 Electrical Measure Systems

### 2.5.1 ZEM-3– Seebeck coefficient & Resistivity

In this study, it can measure samples' seebeck coefficient and electrical resistivity by ZEM-3 in the same time. Two thermocouples in the center (Fig.2.12) which can measure temperature and voltage difference and calculate the seebeck coefficient by

$$S = \frac{\Delta V}{\Delta T} \quad (2.5)$$

Resistance was measured by four-probe measure through relative between  $R$  and  $\rho$  calculation to obtain the resistivity.

$$\rho = R \frac{A}{L} \quad (2.6)$$

where,  $A$  is the cross-section of the sample,  $L$  is the distance between two central thermocouple. The measure temperature  $T$  was measured by temperature of upper and downer thermocouple,  $T_h$  and  $T_c$ , therefore,  $T$  was calculated by

$$T = \frac{T_h + T_c}{2} \quad (2.7)$$

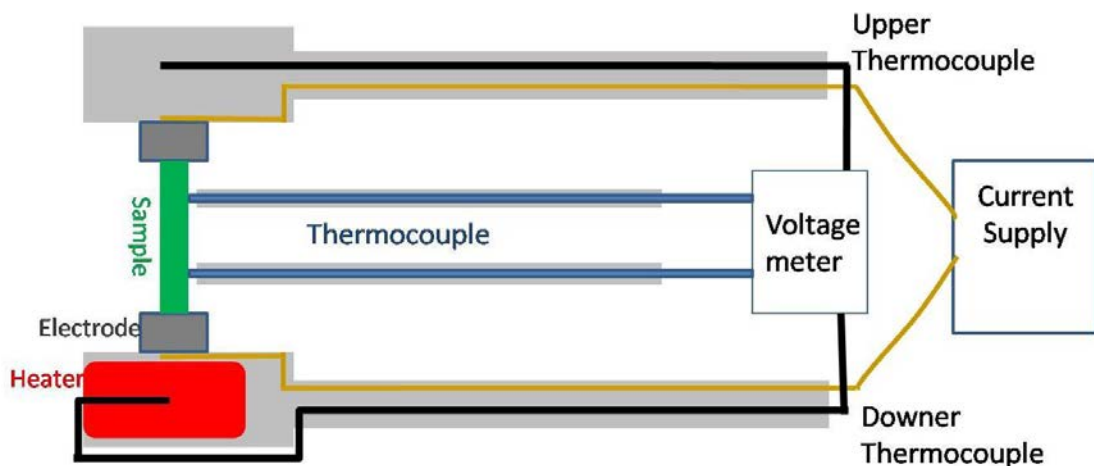


Fig. 2.12 Diagram of ULVAC ZEM-3 measured parts

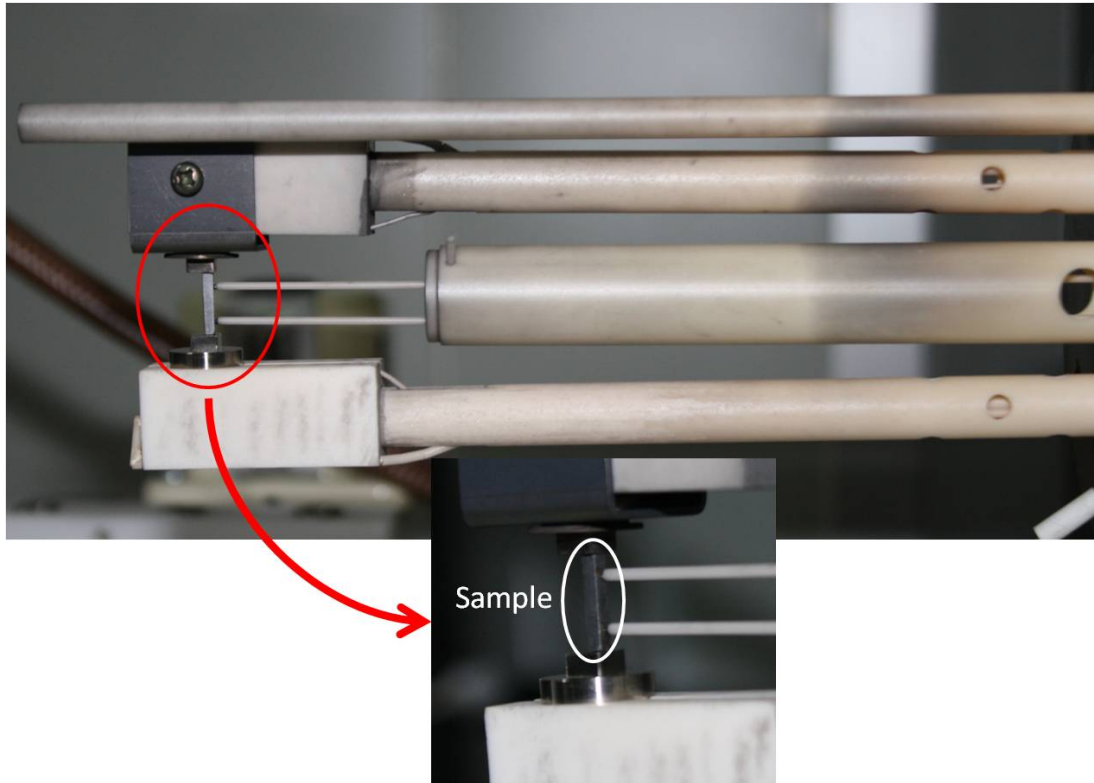


Fig. 2.13 Real setup of ULVAC ZEM-3 measured parts

Firstly, put the sample (2 mm(W) x 2 mm (L) x h mm(H)) between upper and downer electrode with the right thermocouple distance (3, 6 or 8 mm) to attach sample(Fig.2.13). Then, measuring the I-V curve to check the contact is good or not. Secondly, first pumping for the measured chamber at -0.1 Mpa after that flow gas helium into chamber back to normal pressure next is do the second pumping over than 10 minutes to make sure the pressure below than -0.1 MPa afterwards flow the helium again to -0.09MPa be the exchange gas. Finally, set the parameter to software such as temperature range, delta T (for seebeck measurement) and sample's scale. Thereupon, ZEM-3 will measure  $S$  and  $\rho$  automatically.

## 2.5.2 Hall Effect

In 1879, *Edwin Hall* discovered the Hall Effect which is the production of a Hall voltage across an electrical conductor, transverse to an electric current in the conductor and a magnetic field perpendicular to the current. The Hall Effect comes about due to the nature of the current in a conductor. Current consists of the movement of many small charge carriers, typically electrons and holes. If an electric current flows through a conductor in a magnetic field, the magnetic field exerts a transverse force on the moving charge carriers which tends to push them to one side of the conductor. A buildup of charge at the sides of the conductors will balance this magnetic influence, producing a measurable voltage between the two sides of the conductor which is called Hall voltage  $V_H$  follow as:

$$F_m = ev_d B = \frac{eIB}{neA}, F_e = \frac{V_H e}{W} \quad (2.8)$$

$$F_m = F_e, V_H = \frac{IB}{ned} \quad (2.9)$$

$$n = \frac{IB}{edV_H} \quad (2.10)$$

where,  $e$  is a electron charge constant,  $I$  is the current,  $B$  is the magnetic field,  $W$  is the width of the sample,  $d$  is the thickness of sample,  $A$  is the cross-section ( $W \times d$ ) of sample and  $n$  is the carrier concentration.



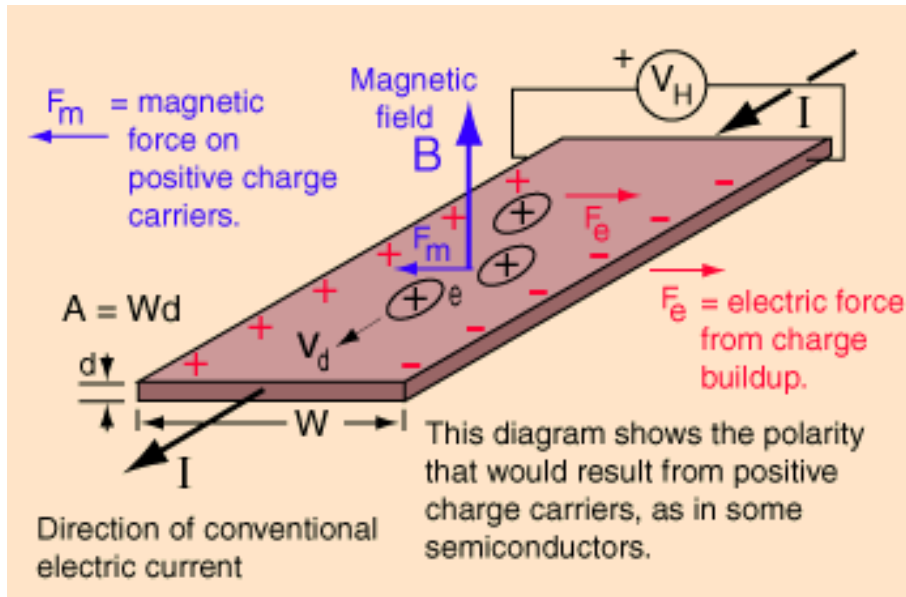


Fig. 2.14 Diagram of Hall effect measurement.

In this study, it will discuss the relative between thermoelectric properties and carrier concentration. So, measure the concentration by PPMS with the magnetic field 9T and -9T to modify the  $V_H$  wire connection non-straight (can't measure at the same cross-section). So, the Hall voltage is getting by

$$V_H = \left| \frac{V_H(\text{with } 9\text{T}) - V_H(\text{with } -9\text{T})}{2} \right| \quad (2.11)$$

## 2.6 Spark Plasma Sintering

The SPS process features a very high thermal efficiency because of the direct heating of the sintering mold and stacked powder materials by large spark pulse

current. It can easily consolidate a homogeneous, high-quality sintered compact because of the uniform heating, surface purification and activation made possible by dispersing the spark point. The theory behind it is that there is a high-temperature or high-energy plasma that is generated between the gaps of the powder materials; materials can be metals, inter-metallic, ceramics, composites and polymers. Using a DC pulse as the electrical current, spark plasma, spark impact pressure, joule heating, and an electrical field diffusion effect would be created.[3] Through various experiments it has been found that in order to design the mechanical properties of new material, controlling the grain size and its distribution, amount of distribution and other is pinnacle.

Fabricate the sample's powders which are three kinds of powders. Firstly, it is pure bulk powders which were fabricated through ball milling with the condition, 500 rpm for 30 minutes and pause 10 minutes repeat 20 times. Secondly, those were fabricated pure nanoparticles by hydrothermal method from Dr. Chang in M.K.Wu's lab. Finally, mix the bulk powders and nanoparticles with the designated ratio. Next, load the sample's powder into mold. Put the graphite mold which has the powder inside into Spark Plasma Sintering (SPS), afterwards pump SPS chamber below 6 Pa. Afterwards, sinter the powder to ingot with adaptive conditions (Table 2.4).



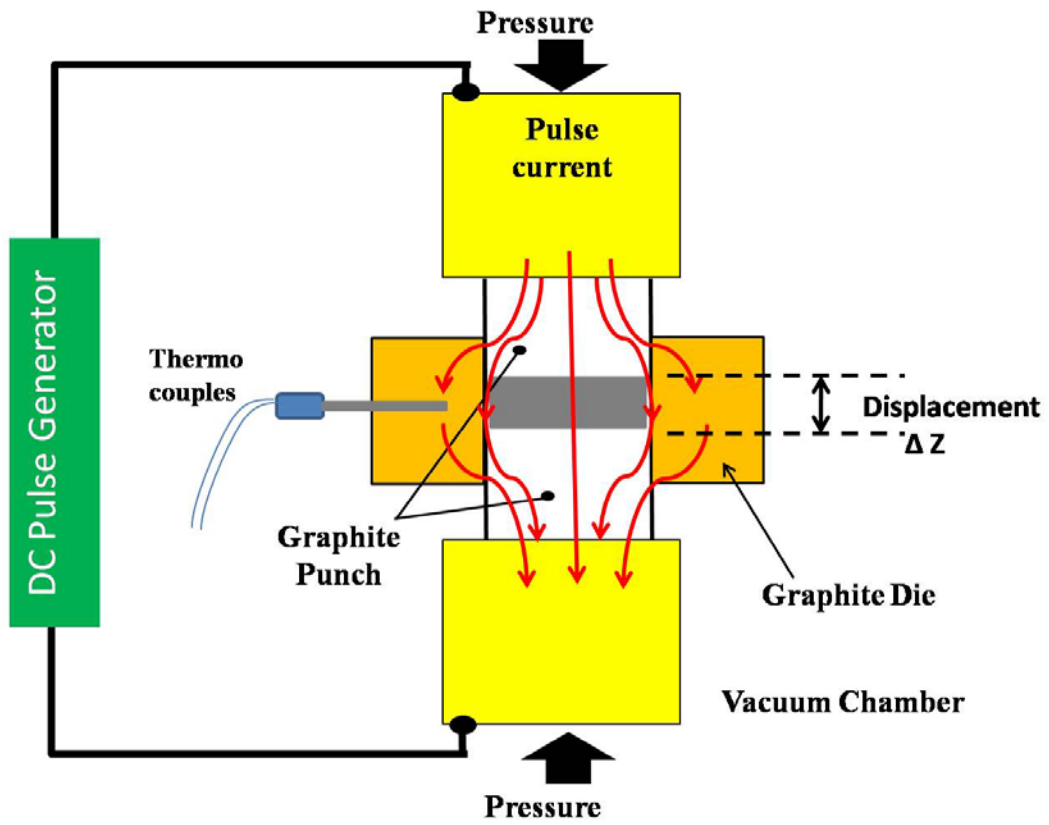


Fig. 2.15 Diagram of spark plasma sintering ON-OFF pulsed current path

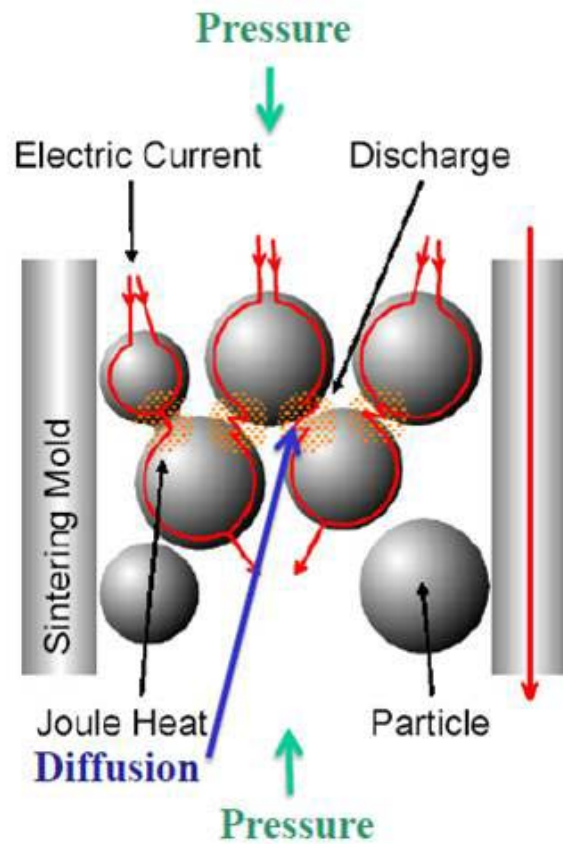


Fig. 2.16 Pulsed current flow through powder particles

Table 2.4 SPS conditions for every sample in this study

Sample	Sintering Temperature (°C)	Pressure (Mpa)	Heating Rate (K/min)	Sintering Time (min)
<b>Cu<sub>0.01</sub>Bi<sub>2</sub>Te<sub>2.7</sub>Se<sub>0.3</sub> Bulk</b>	<b>400</b>	<b>50</b>	<b>50</b>	<b>5</b>
<b>Powder</b>				
<b>Nanoparticles</b>				
<b>Bulk Powder (BP)+ 10 wt% NPs</b>				
<b>BP+20 wt% NPs</b>				
<b>BP+30 wt% NPs</b>				
<b>BP Bi<sub>0.45</sub>Sb<sub>1.55</sub>Te<sub>3</sub></b>	<b>400</b>	<b>50</b>	<b>50</b>	<b>5</b>
<b>BP Bi<sub>0.5</sub>Sb<sub>1.5</sub>Te<sub>3</sub></b>				

# Chapter 3 Results and Discussions

## 3.1 $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$ Nanocomposites

### 3.1.1 Analysis

The nanocomposites presented in this study were prepared using  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  n-type bismuth telluride based material cause that cause that has the evidence to show the  $\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  doping around 1 % Cu can reduce the Electrical resistivity.[7][8]. The composite microstructure and composition, as well as the effects of the nanoparticles on the thermal and electrical transport properties are presented below, with a focus on the effect of the nanoparticles on the thermoelectric efficiency of the composite.

After Bridgman growth, the bulk and powders which are from ball milling were confirmed by powder x-ray diffraction (XRD) (Fig.3.1), and the particle size and morphology was found by scanning electron microscopy(SEM) to be spherical-irregular, with sizes from 20 nm to 5  $\mu\text{m}$  (Fig. 3.3) and confirm the atomic percentage by SEM-EDX (Fig.3.2). From the Fig.3.2 it doesn't find Cu signal that the reason is maybe from the rare doping is difficult to detect by EDS resolution. Compare with Fig.3.4, 3.5 and 3.6 that the amounts of nanoparticle increase by the doping percentage obviously.

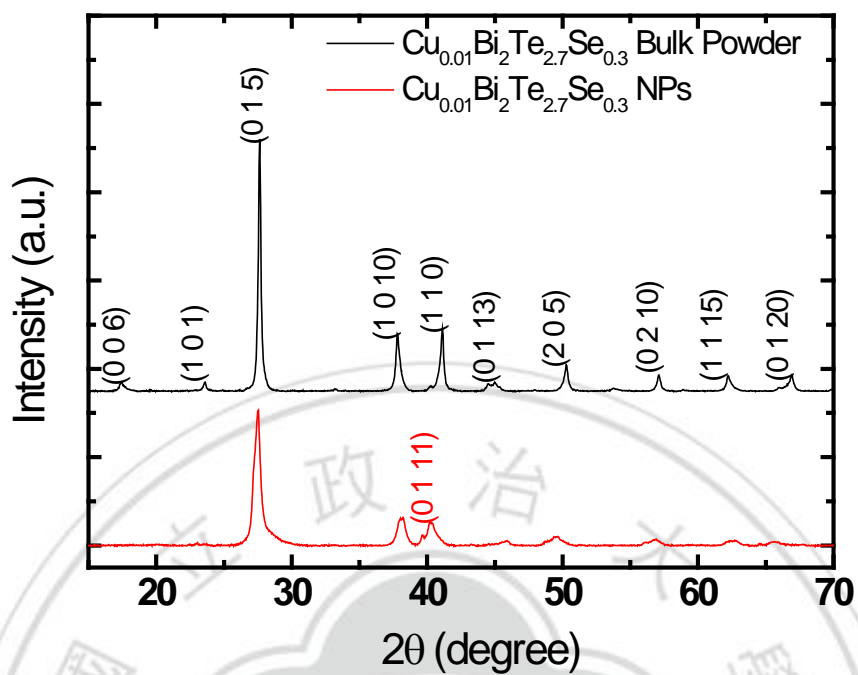


Fig.3.1 X-ray diffraction pattern of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  bulk powder and nanoparticles

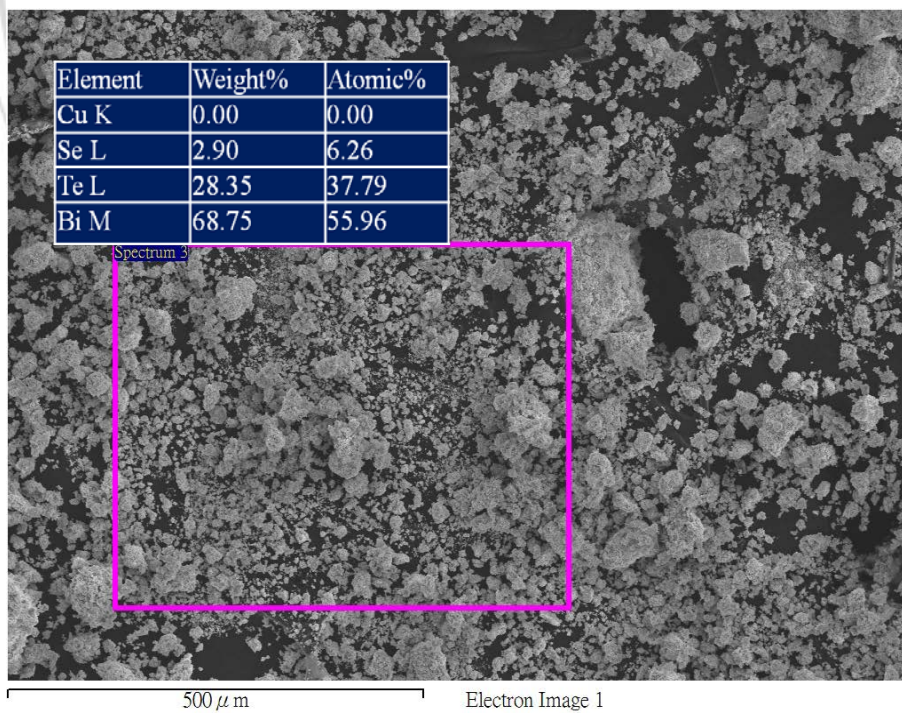


Fig.3.2 EDX of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  NPs to show the atomic percentage.



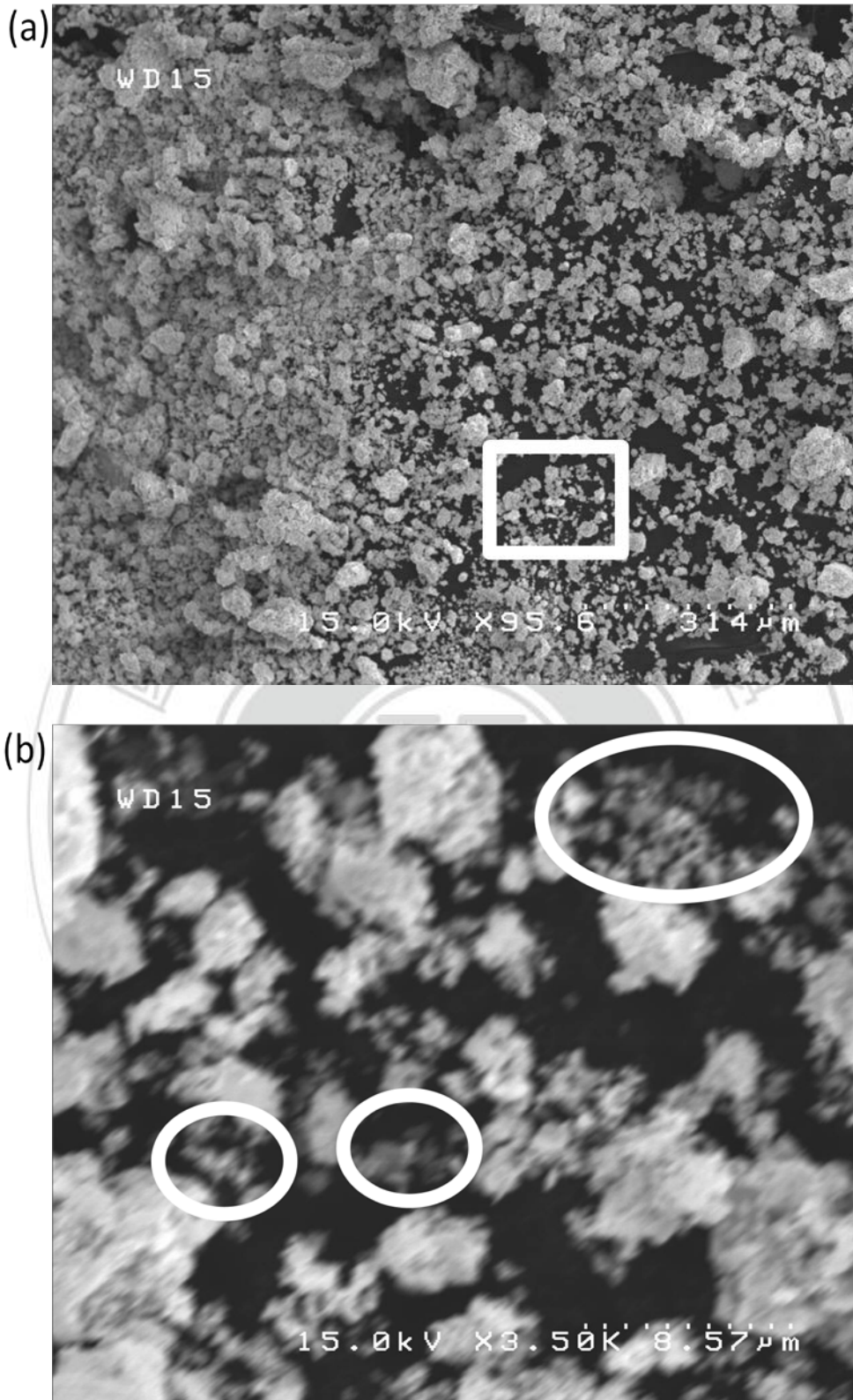


Fig.3.3 SEM images of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  nanoparticles prepared by hydrothermal a) significantly smaller grain sizes b) Close view of portion from (a), nanoparticles were observed in white region.

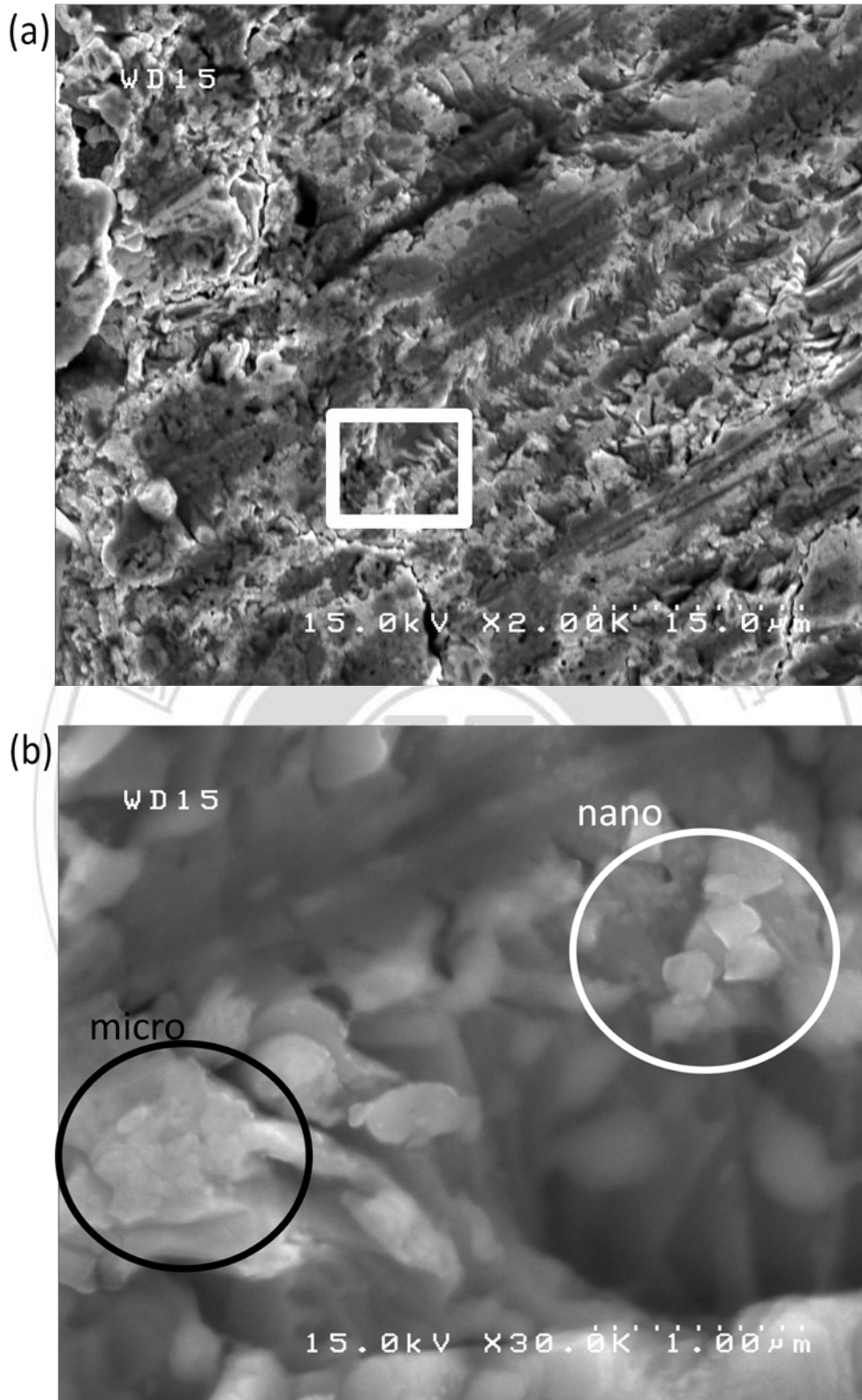


Fig.3.4 SEM images of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  nanocomposite 10 wt% prepared by ball milling, hydrothermal and SPS. A) Significantly smaller grain sizes b) Close view of portion from (a).

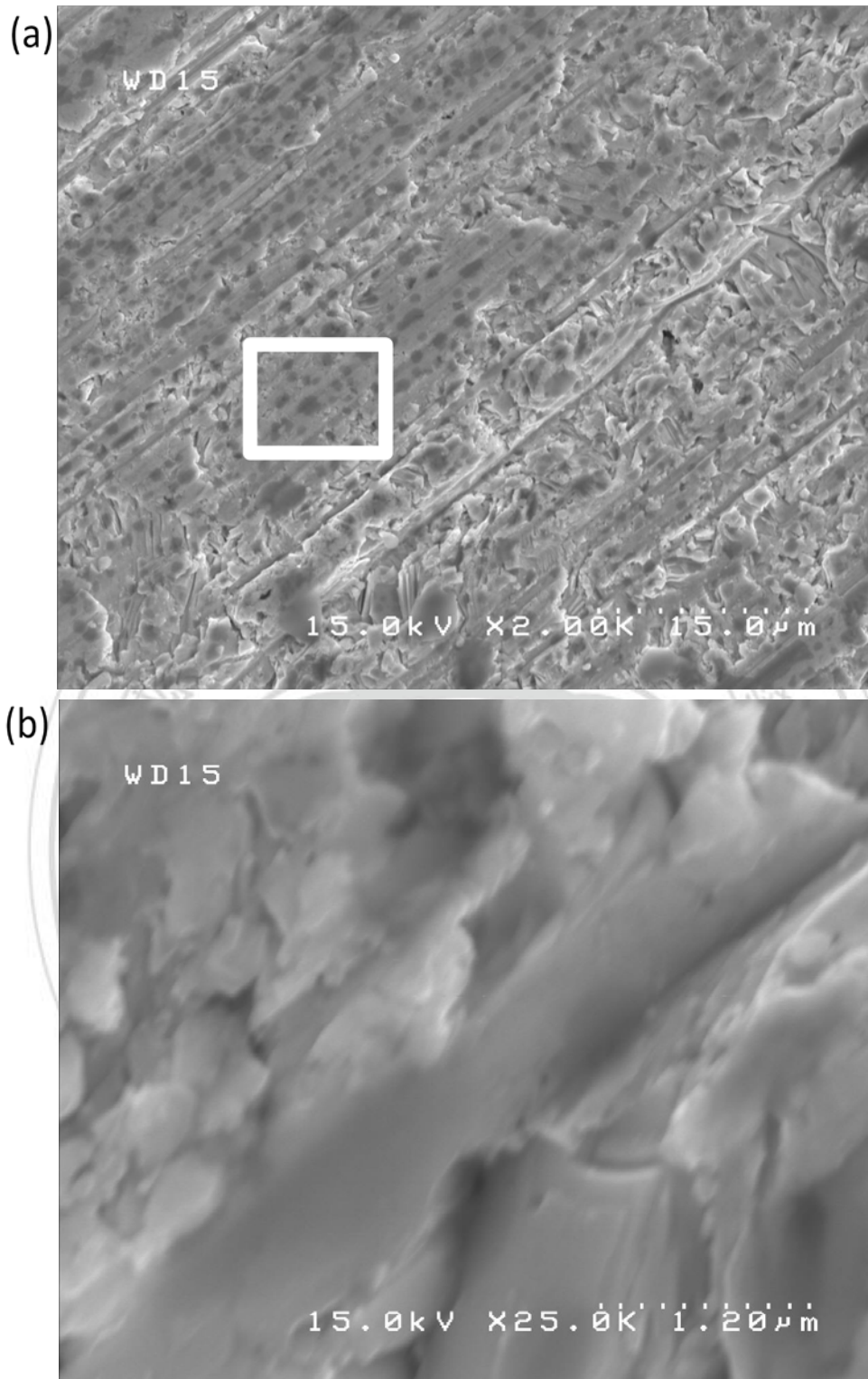


Fig.3.5 SEM images of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  nanocomposite 20 wt% prepared by ball milling, hydrothermal and SPS. A) Significantly smaller grain sizes b) Close view of portion from (a).



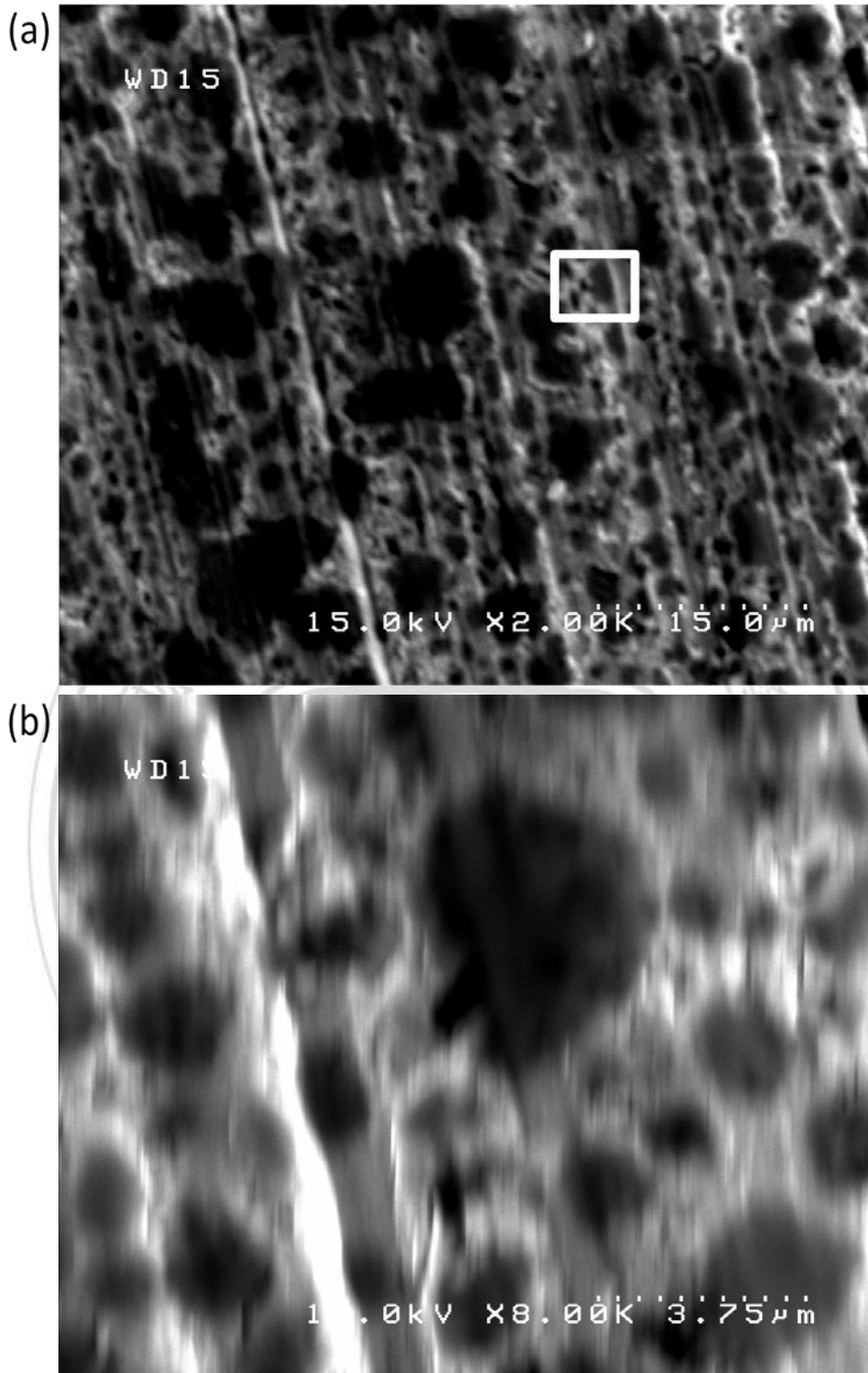


Fig.3.6 SEM images of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  nanocomposite 30 wt% prepared by ball milling, hydrothermal and SPS. A) Significantly smaller grain sizes b) Close view of portion from (a).



### 3.1.2 Thermal properties

Thermal properties are including thermal diffusivity  $D$ , specific heat  $C_p$ , and density  $d$ , and the thermal conductivity  $\kappa$  relative with  $D$ ,  $C_p$  and  $d$ , follow as:

$$\kappa = D \times C_p \times d \quad (3.1)$$

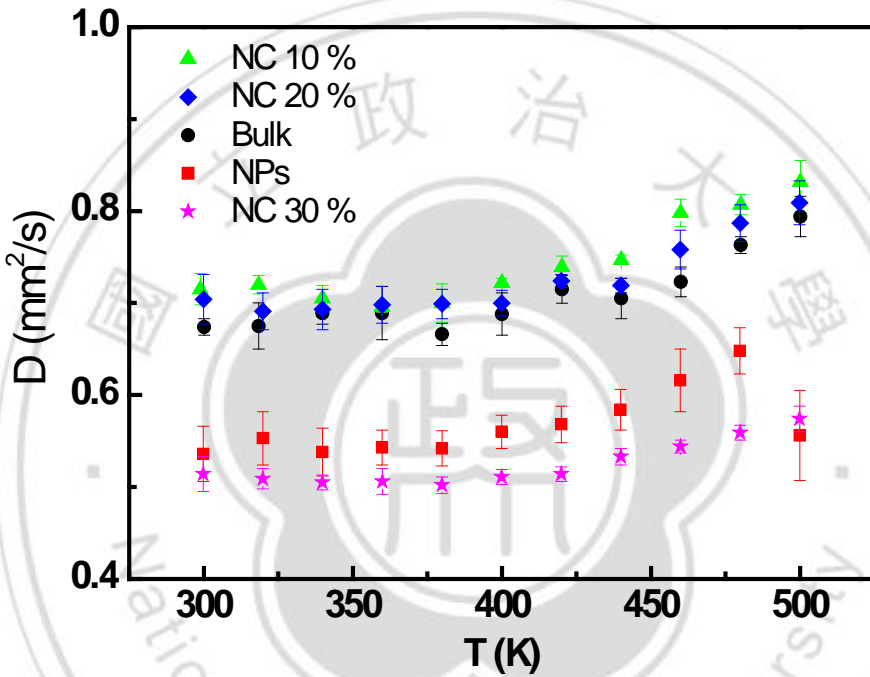


Fig.3.7 Thermal diffusivity versus temperature of n-type  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$

According to the Debye model which is a method developed by *Peter Debye* in 1912 that is shown about the specific heat low temperature and high temperature limitation as following formula.

$$\frac{U}{N_K} = 9T \left(\frac{T}{T_D}\right)^3 \int_0^{\frac{T_D}{T}} \frac{x^3}{e^x - 1} dx = 3TD_3 \frac{T_D}{T} \quad (3.2)$$

Where,  $U$  is energy,  $N_K$  is,  $T_D$  is the Debye temperature and  $D_3$  is the third Debye function. Then, differentiating with respect to  $T$ , it will show the dimensionless heat capacity.

$$\frac{C_v}{N_K} = 9 \left(\frac{T}{T_D}\right)^3 \int_0^{\frac{T_D}{T}} \frac{x^4 e^x}{(e^x - 1)^2} dx \quad (3.3)$$

This formula treats the Debye model at all temperature.

In low temperature limit, the temperature of a Debye solid is said to be low if  $T \ll T_D$ , the (eq.) can simplify leading to

$$\frac{C_v}{N_K} \sim 9 \left(\frac{T}{T_D}\right)^3 \int_0^{\infty} \frac{x^4 e^x}{(e^x - 1)^2} dx = \frac{12\pi^4}{5} \left(\frac{T}{T_D}\right)^3 \quad (3.4)$$

It shown the specific is directly proportional to  $T^3$ .

For high temperature limit, the temperature of a Debye solid is said to be low if  $T \gg T_D$ , using the  $e^x - 1 \sim x$ , if  $|x| \ll 1$

$$\frac{C_v}{N_K} = 9 \left(\frac{T}{T_D}\right)^3 \int_0^{\frac{T_D}{T}} \frac{x^4}{x^2} dx = 3 \quad (3.5)$$

This is the *Dulong–Petit* law, and is fairly accurate although it does not take into account anharmonicity, which causes the heat capacity to rise further. The total heat capacity of the solid, if it is a conductor or semiconductor, may also contain a non-negligible contribution from the electrons. It shows the specific heat is constant closely when the temperature over than Debye temperature that has a lot of experiments show room temperature is already over than  $T_D$ . And this matrix material is just the  $\text{Bi}_2\text{Te}_3$  rare doping. So, it can assume the specific heat is a constant. In this study, it can use 0.2 which is the specific heat of  $\text{Bi}_2\text{Te}_3$  to be the  $C_p$  when the temperature over than room temperature.

Table3.1 Density of all  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  samples in this study.

	Bulk	Nanoparticles 100 % NPs ingot	Nanocomposite 10 wt% NPs doped	20 wt%	30 %
Density ( $\text{g}/\text{cm}^3$ )	7.7278	6.4107	7.5864	7.4642	7.1243

According to eq. [2.2],  $\kappa$  can be calculated by multiply D, C and d.

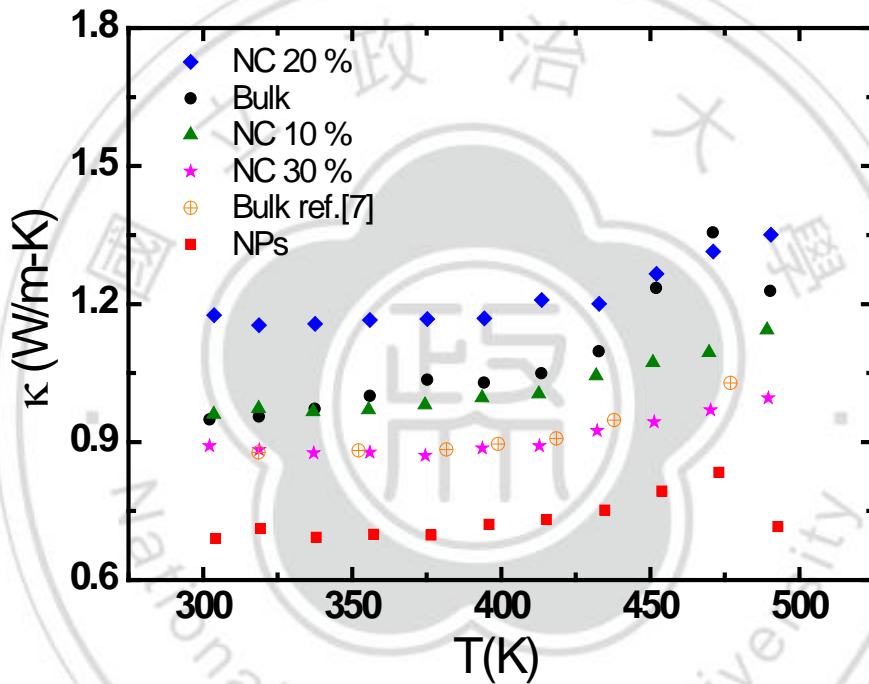


Fig.3.8 Thermal conductivity of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  bulk, NPs, NC 10% 20% and 30% versus temperature

From the Fig.3.8, it can be observed the thermal conductivity of nanoparticles lower than bulk obviously when the temperature over than 420 K. And the result 10 wt-% nanoparticle doped is similar with the bulk powder. Although increasing the doped percentage to 20% that has the largest  $\kappa$ . When doping more nanoparticles to

30% which has the smallest thermal conductivity obviously. So, it will shows a result that the doped ratio needs over than 20 wt% can improve the thermal properties for  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$ .

### 3.1.3Electrical properties

Electrical resistivity (also known as resistivity, specific electrical resistance, or volume resistivity) is a measure of how strongly a material opposes the flow of electric current. A low resistivity indicates a material that readily allows the movement of electric charge. In the definition, the resistivity show as:

$$\rho = \frac{E}{J} \quad (3.6)$$

where,  $E$  is the electrical field and  $J$  is current density. In this study, the resistance is calculated through resistance measure with four-probe measure by ZEM-3.

$$\rho = R \frac{A}{L} \quad (3.7)$$

Fig.3.9 shows the electrical resistivity vs. temperature data for this series. The curvature of the trend for each different  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  shows change. It shows the resistivity of nanoparticles ingot lower than bulk about 100 % at 330K, and the composite structure lower than nanoingot and bulk around 70 % and 170 %. This reduction was caused mainly by the presence of nanostructured regions existing within the samples and through the SPS process can maintain the resistivity even reduction.

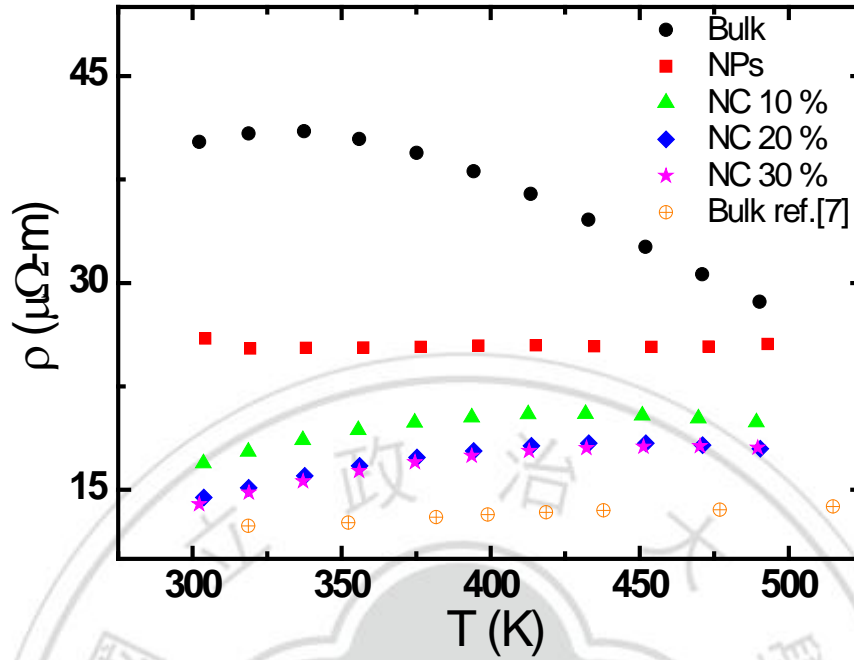


Fig.3.9 Electrical resistivity of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  materials versus temperature

Fig.3.10 shows the Seebeck coefficient vs. temperature data for this series. The curvature of the trend for each different  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  shows change, and the Seebeck coefficient of the nanocomposites have a mean value about  $-168 \pm 2 \mu\text{V/K}$  at 430 K, reduction in magnitude of approximately  $14 \mu\text{V/K}$  and growth in magnitude of approximately  $28 \mu\text{V/K}$  compared to the commercial bulk and pure nanoparticles ingot.

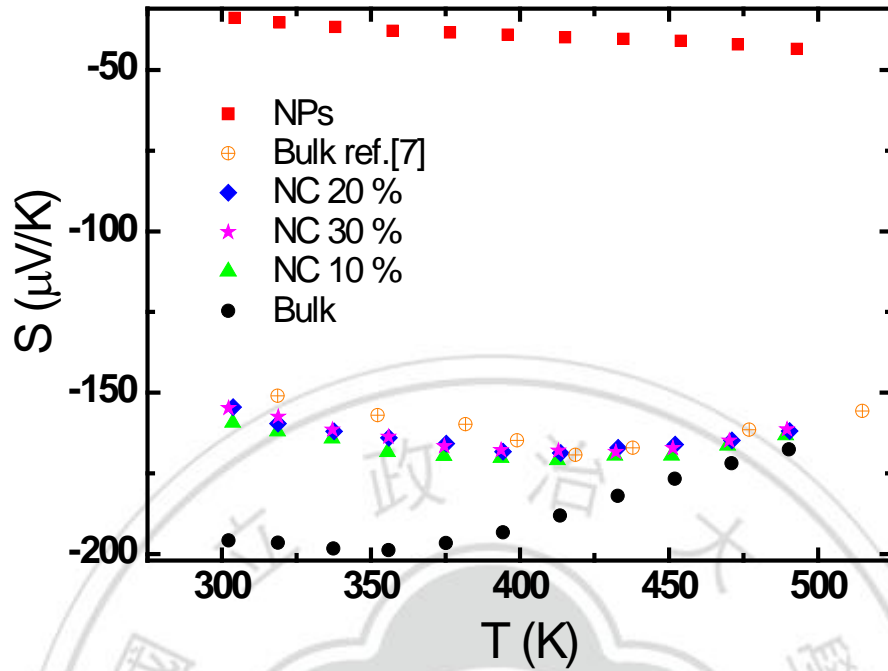


Fig.3.10 Seebeck coefficient of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  materials versus temperature

### 3.1.4 Figure of Merit

From Fig.3.11, getting the best  $ZT$  value is 0.74 at 430K by  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  nanocomposite with 30 wt% doped. And the each nanocomposite has the better thermoelectric properties than bulk and nanoingot. So, it can benefit the thermoelectric properties about 100% by nanocomposite. This enhancement was caused mainly by the presence of nanostructured regions existing within the samples lowered thermal conductivity due to the significant number of grain boundaries, short phonon mean free path and lattice mismatch.

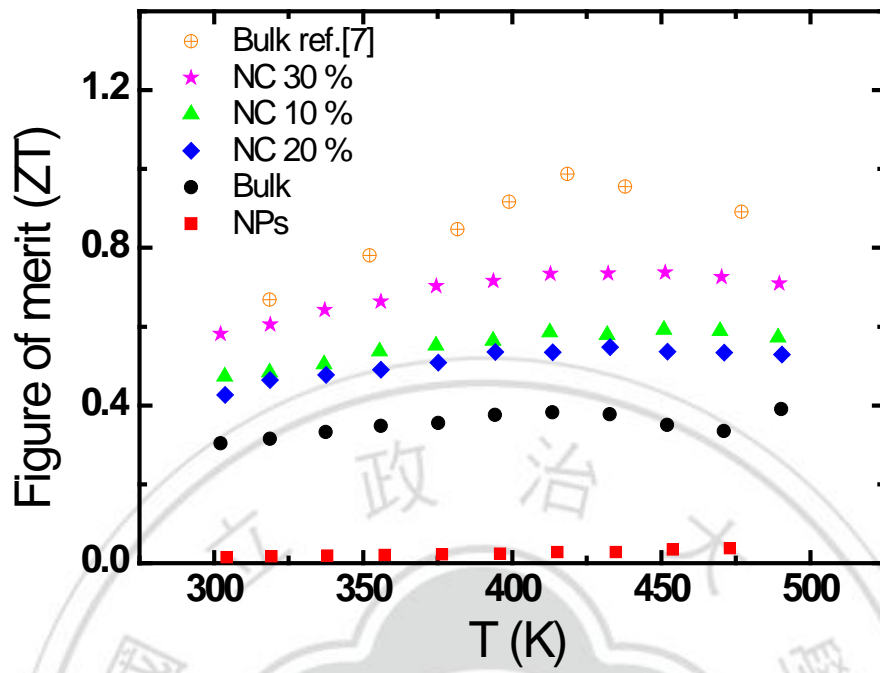


Fig.3.11 ZT value of  $\text{Cu}_{0.01}\text{Bi}_2\text{Te}_{2.7}\text{Se}_{0.3}$  materials versus temperature

## 3.2 $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$ ( $x=0.4, 0.45, 0.5$ and $0.6$ )

### 3.2.1 Analysis

In normally, the  $x=0.5$  is a famous TE material for sale. But that has a investigation to show the  $x=0.45$  is better than 0.5. [9][10] The samples presented in this study were prepared using  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ( $x=0.4, 0.45, 0.5$  and  $0.6$ ) p-type bismuth telluride based material.

After Bridgman growth, the ingots were confirmed by XRD (Fig.3.12), and Fig.3.13, 3.14, 3.15 and 3.16 shown in relative ratios that are consistent with the composition of the matrix material by SEM-EDX. The EDX has resolute limitation around 3-5%, so rare doped is difficult to different. According to analysis data by EDX, it shows the relative ratios are close to setup at beginning.

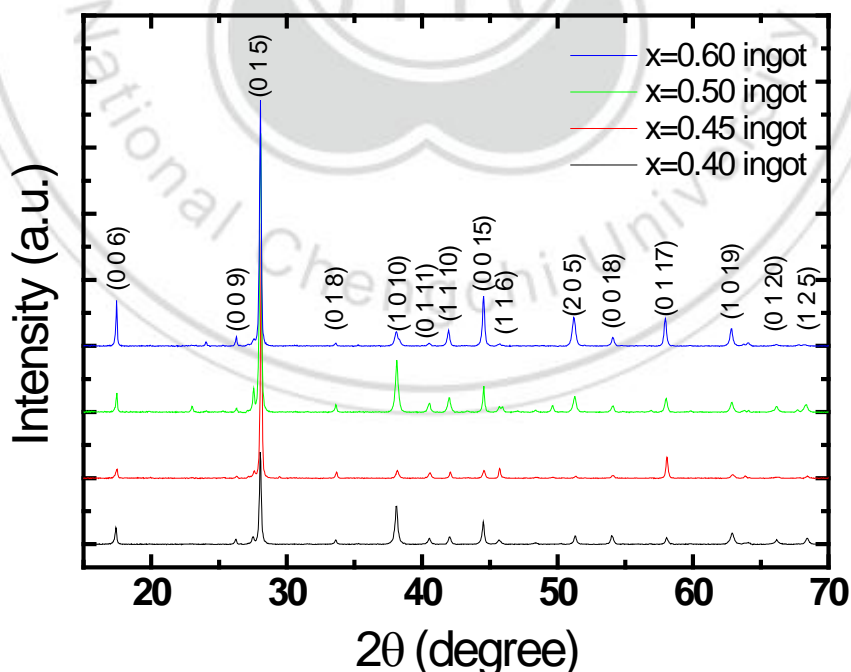


Fig.3.12 X-ray diffraction pattern of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ingots( $x=0.4, 0.45, 0.5, 0.6$ )



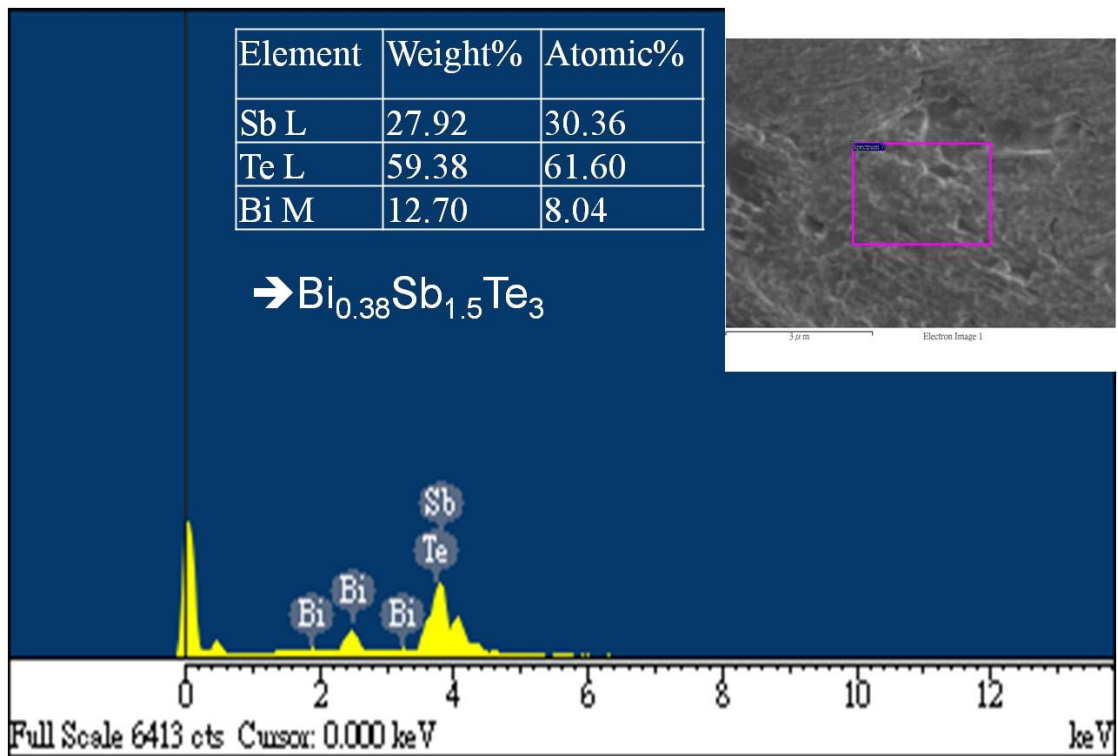


Fig.3.13 EDX of  $\text{Bi}_{0.4}\text{Sb}_{1.6}\text{Te}_3$  to show the atomic percentage.

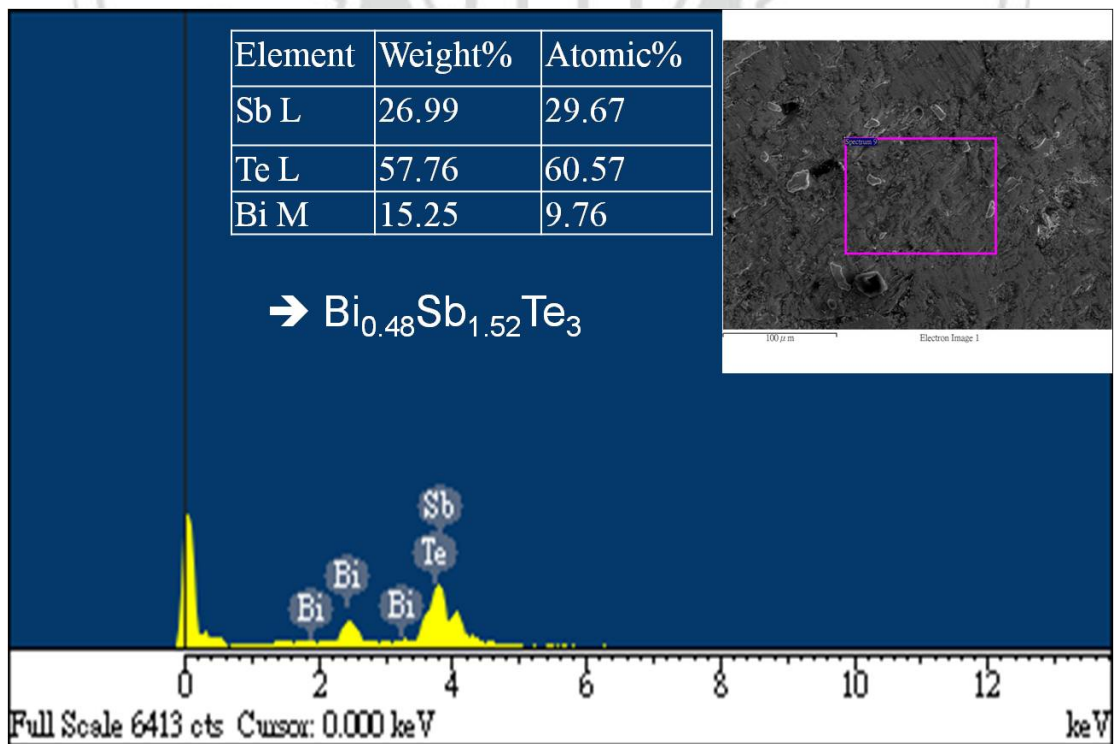


Fig.3.14 EDX of  $\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3$  to show the atomic percentage

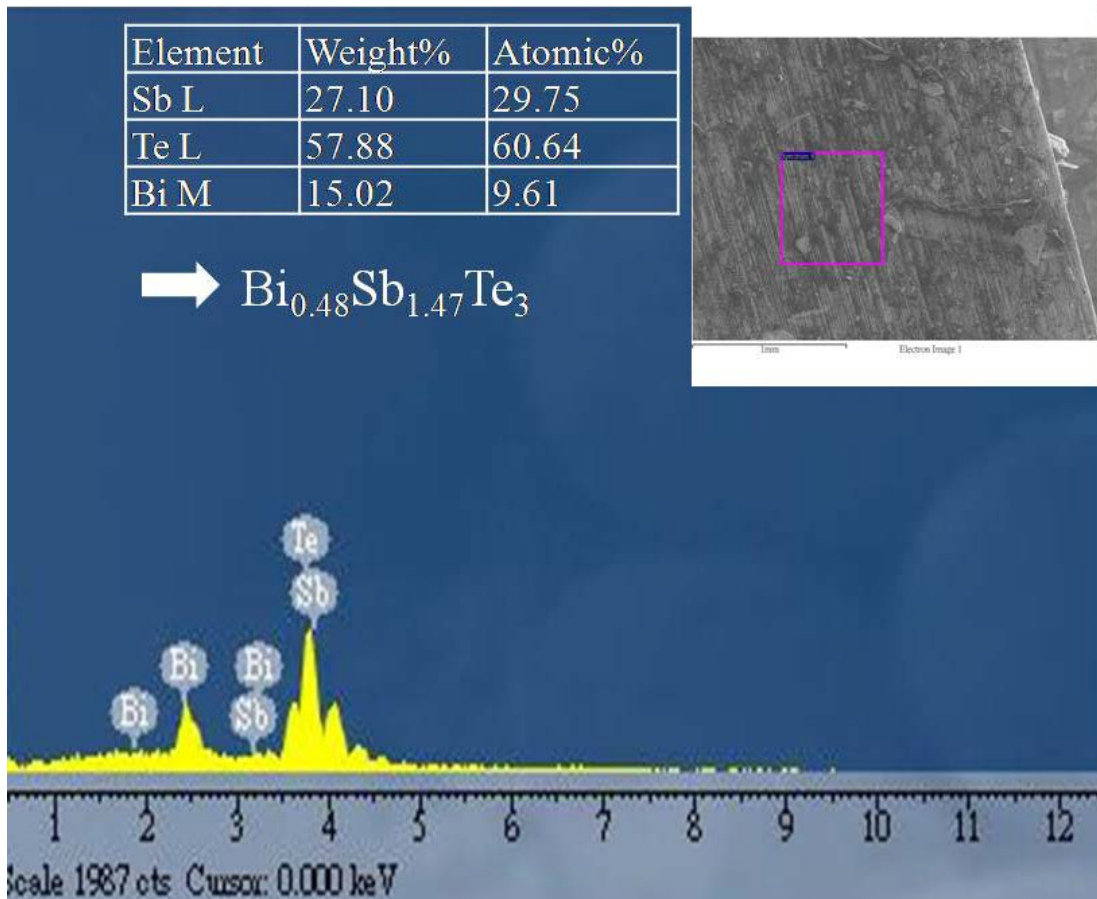


Fig.3.15 EDX of  $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$  to show the atomic percentage

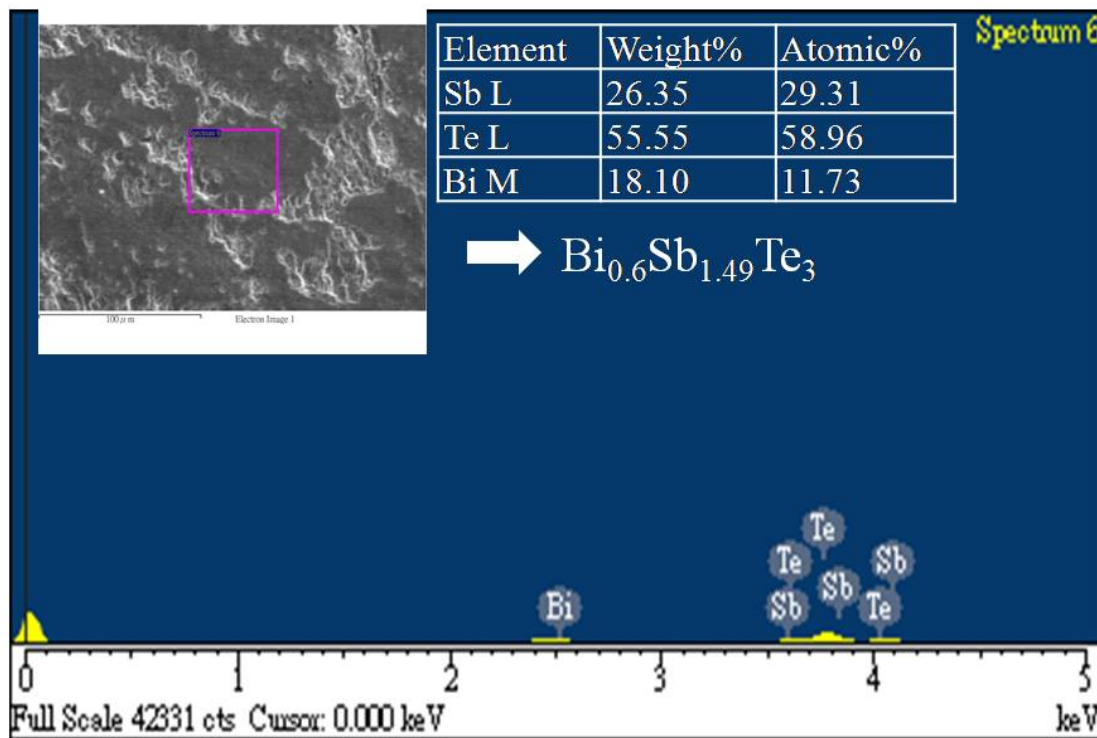


Fig.3.16 EDX of  $\text{Bi}_{0.6}\text{Sb}_{1.4}\text{Te}_3$  to show the atomic percentage

### 3.2.2 Thermal properties

Thermal properties are including thermal diffusivity  $D$ , specific heat  $C_p$ , and density  $d$ , and the thermal conductivity  $\kappa$  relative with  $D$ ,  $C_p$  and  $d$ , follow as:

$$\kappa = D \times C_p \times d \quad (3.7)$$

According to Fig.3.17, it can find the relative thermal diffusivity,  $D$ , increase following the ratio with Bi reduction when the  $x$  below 0.5. And there have a transition when the  $x$  above 0.5 that the shape of curve is different with  $x=0.4$ , 0.45 and 0.5 obviously. Maybe it shows if  $x$  larger than 0.5 that have some physical properties are changed.

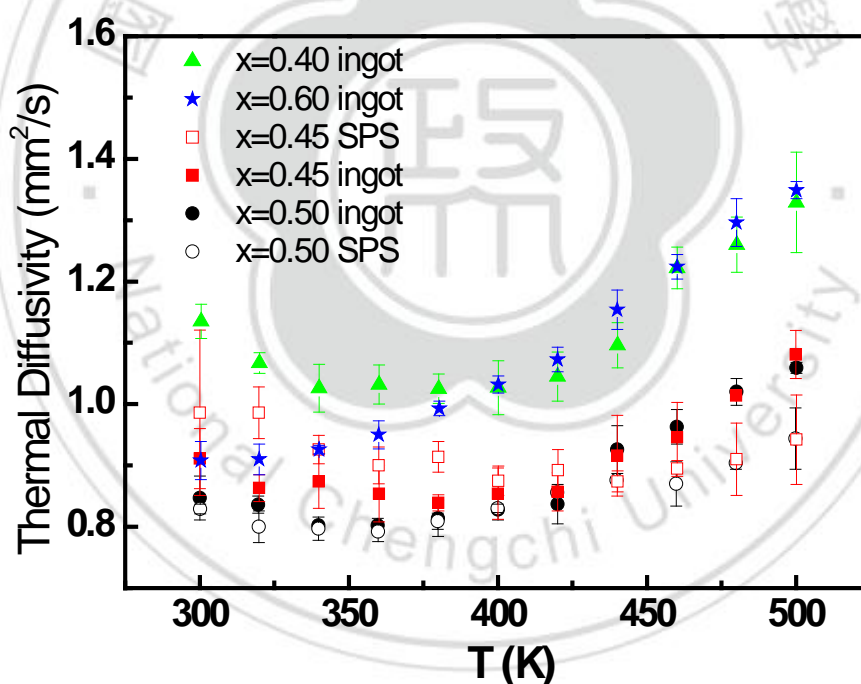


Fig.3.17 Thermal diffusivity of p-type  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  versus temperature

According to *Dulong–Petit law*, the specific heat is constant closely when the temperature over than Debye temperature. Therefore, it can assume the specific heat is a constant. The specific heat of  $\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3$  from 125 to 460 K is shown in

Fig.3.18a and compared with Fig.3.18b which is the data from reference[6] with  $x=0.5$  which shows the specific heat close near to a constant around 0.23 when the temperature over than  $-50\text{ }^{\circ}\text{C}$ , then, it can assume  $C_p$  is the constant 0.23 over than 300 K. Although the results of Fig.3.18a and Fig.3.18b are not closely, but, in this study, it still uses the real data to replace into  $C_p$  value.

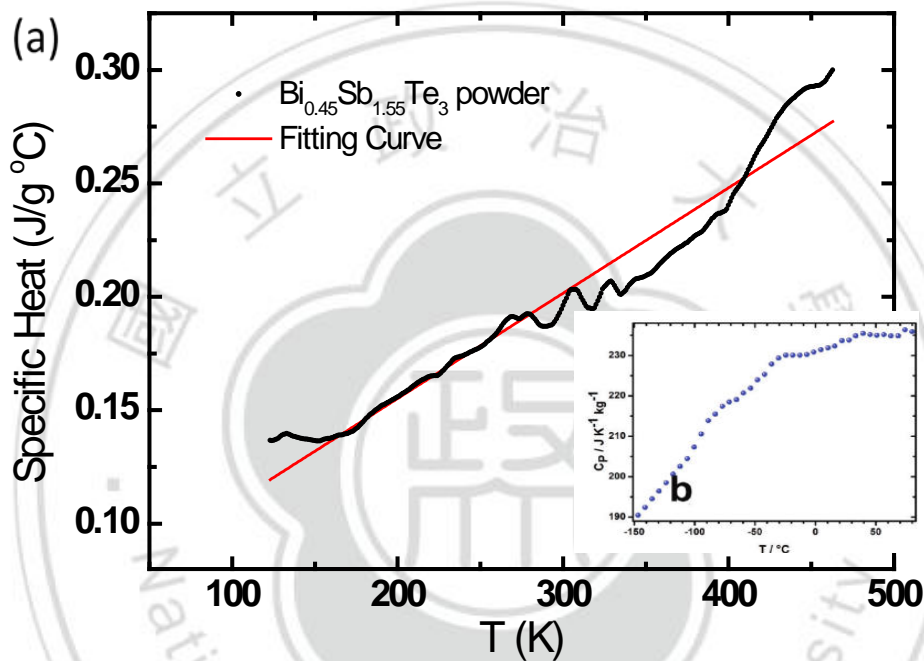


Fig.3.18 a) The specific heat of  $\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3$  versus temperature b) Reference of  $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$  [6]

The density can be measured by Archimedes principle. From the table3.2, it show the density and the ratio of Bi element are direct proportion obviously, because the mass of Bi is heavier than Sb. For  $x=0.5$  SPS composite about 88 % compare to ingot, but when  $x=0.45$  the SPS composite just 77 % with the same sintering condition.

Table3.2 Density of every  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  samples

Ingot	x=0.4	x=0.45	x=0.5	x=0.6
Density ( $\text{g}/\text{cm}^3$ )	6.468	6.643	6.748	6.897
SPS pellet		x=0.45	x=0.5	
Density ( $\text{g}/\text{cm}^3$ )		5.126	5.925	

Following eq. (2.2),  $\kappa$  can be calculated by multiply  $D$ ,  $C$  and  $d$ .

From the Fig.3.19, it can be observed the thermal conductivity of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  depend on the ratio of Bi, the thermal conductivity and  $x$  value are inverse proportion when the  $x < 0.5$ . Combination the results of  $D$  and  $\kappa$ , there are also shown if the  $x$  over than 0.5, then, the trend has a little change which is about the minimum of thermal conductivity and diffusivity were moved from 360 to 300 K. And it can be observed  $\kappa$  goes lower through SPS process obviously that the main reason is from the increase the phonon scattering because it has more boundaries in the SPS composites.

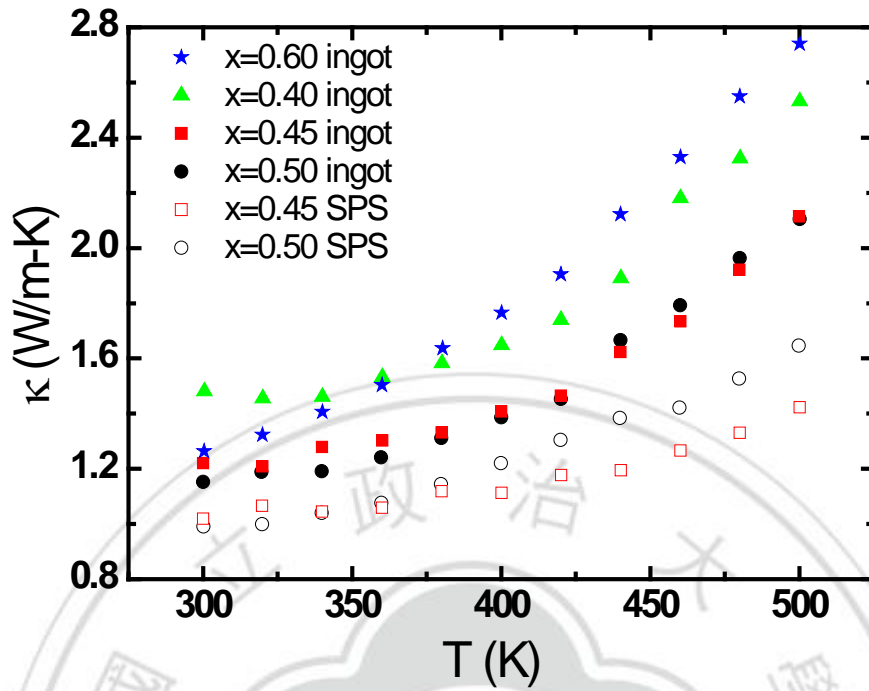


Fig.3.19 Thermal conductivity of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  bulk,  $x=0.4, 0.45, 0.5$  and  $0.6$  versus temperature

### 3.2.3 Electrical properties

Fig.3.20 shows the electrical resistivity vs. temperature data for this series. The curvature of the trend for each different  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  shows change. In normally, the SPS process can maintain or reduce the resistivity and reduce the thermal conductivity. Compare between Fig.3.19 and Fig.3.20,  $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$ 's result shows that decrease the  $\kappa$  and maintain the resistivity through SPS fabrication. Next, in the  $\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3$ 's data, even thermal conductivity is reduced, but the resistivity larger about 10 times.



The mainly reason maybe from the density which is lower than  $x=0.5$  about 13.5 %. The effect likes impurity diffusion in the sample, then the electrons passing difficulty. Therefore,  $\rho$  is increase several times. Next, it focus on the curvatures which are differenced to two shapes, the first is  $x=0.4$  and  $0.4$  that trend is linear line similar and the second is  $x=0.45$  SPS,  $0.5$  and  $0.6$  the shape are curve.

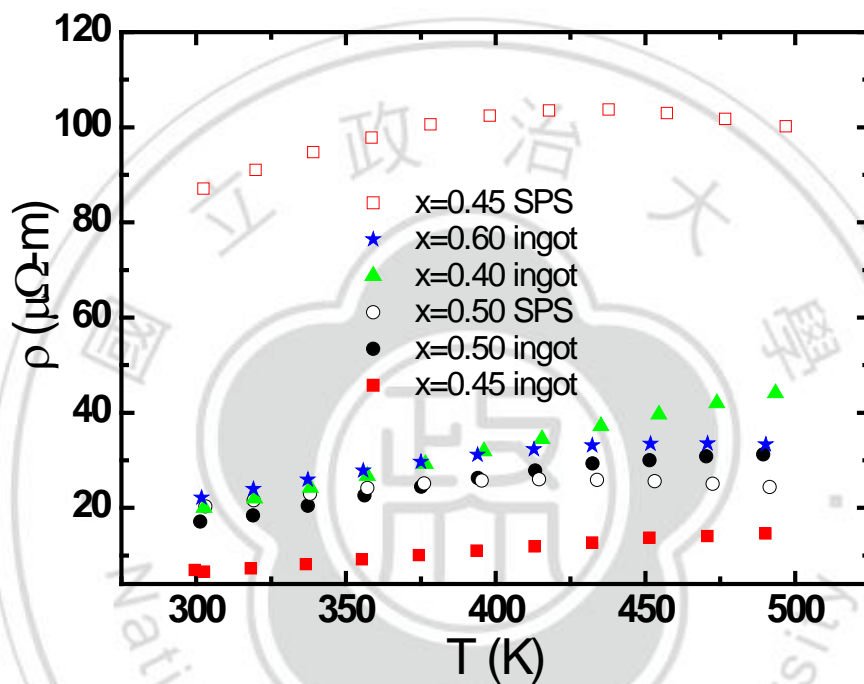


Fig.3.20 Electrical resistivity of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  materials versus temperature

From Fig.3.21 shows the Seebeck coefficient vs. temperature data for this series. The curvature of the trend for each different  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  shows change, and the Seebeck coefficient at 320 K of each  $x$  valued have a range about from 180 to 275  $\mu\text{V}/\text{K}$ , the samples were fabricated by SPS process which the  $S$  are higher than original ingots in evidence. In physics rule, the  $S$  and  $\rho$  are direct proportion and through to compare the results of the  $x=0.45$  and  $0.5$  can observe it obviously. The ingots'  $S$  is not sensitive with the amount of Bi, but the curvature of  $x=0.4$  is different

to others.

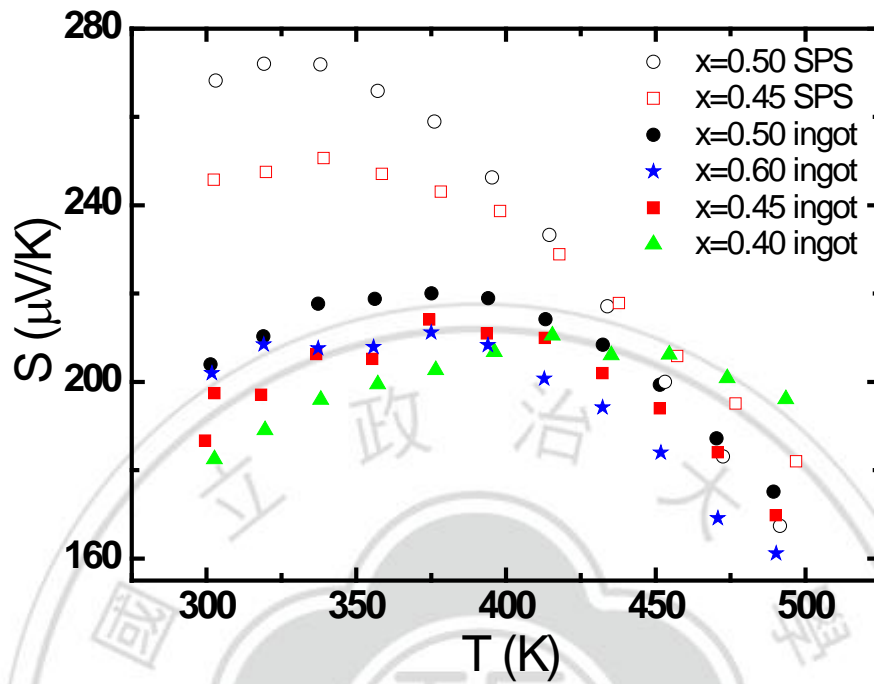


Fig.3.21 Seebeck coefficient of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  materials versus temperature

By Fig.3.22, it shows the carrier concentration of each sample which can explain the reason of the lowest resistivity from  $\text{Bi}_{0.45}\text{Sb}_{1.55}\text{Te}_3$  directly. From this result that it can harvest a conclusion that the  $x=0.45$  ingot's concentration has changed after SPS process. In general, the resistivity is inverse proportion to carrier concentration. Therefore, it compares between Fig.3.20 and 3.22 and the results are also following  $\rho \propto 1/n$ . It is can explain why the  $x=0.45$  ingot has the lowest resistivity because by the highest carrier concentration.



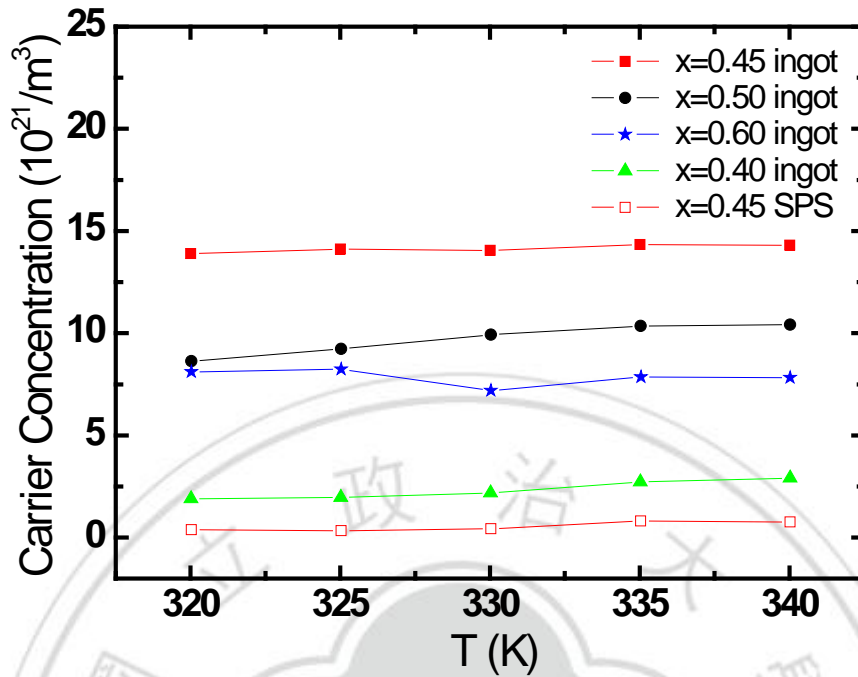


Fig.3.22 The carrier concentrations of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  materials from 320 to 340 K.

### 3.2.4 Figure of Merit

In this study, the best  $ZT$  value 1.46 is obtained at 300K by  $x=0.45$  ingot. Firstly, it focuses on  $x=0.5$  which the composite was fabricated through SPS technique can enhance the  $ZT$  value around 50% from 0.72 to 1.15 at 340K. However, in the other case that the  $ZT$  of  $x=0.45$  composite was decreased after SPS process. Although the result is with lower thermal conductivity and higher Seebeck coefficient, but the mainly problem is from the 10 times larger electrical resistivity, therefore, the figure of merit is smaller around 8 times than the original ingot. Compare the results  $S$  and  $\rho$  that have not a lot differences between  $x=0.4, 0.5$  and  $0.6$ . And the  $ZT$  values of  $x=0.4$

and 0.6 are smaller than  $x=0.5$  that the main reason is from thermal conductivity. The best  $ZT$  is  $x=0.45$  that caused by the lowest electrical resistivity. Then, it discuss between Fig.3.22 and 3.23 that show the result is the sample has the higher  $ZT$  value with the higher carrier concentration.

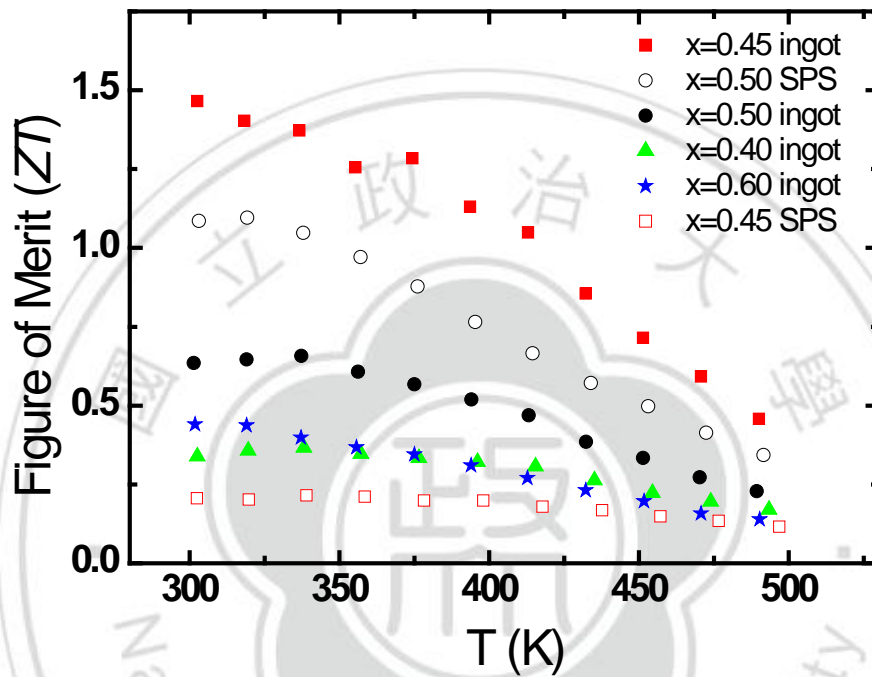


Fig.3.23  $ZT$  value of  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  ( $x=0.4, 0.45, 0.5$  and  $0.6$ ) materials versus temperature

## Chapter 4 Conclusions

This study provides at the first investigation of the effects of nanomaterials upon the thermal and electrical transport properties of nanocomposites formed using favorable thermoelectric(TE) materials as a matrix. The nanocomposites studied herein are also of value for investigating the viability of the spark plasma sintering(SPS) technique for producing such composites, as well as being of benefit for studying viable techniques of nanoparticle growth. While the end results have in most cases not been the formation of nanocomposites that have figures of merit that surpass the bulk materials, the effects of the nanomaterials upon the electrical and thermal properties nevertheless help illuminate interesting new directions for thermoelectric research of nanocomposites. The  $ZT$  value is enhanced around 100% through 30 wt% nanoparticles doping. If the bulk material can fabricate achieving to commercial value about 0.9 like as ref.[7], afterwards, use the nanocomposited method. The  $ZT$  is expected to exceed 1.2 at  $T > 400$  K.

For the other investigation which discussed the effects about  $\text{Bi}_x\text{Sb}_{2-x}\text{Te}_3$  with the different ratios of Bi doping. Firstly, the thermal conductivity has change following the Bi amounts. It shows when the  $x < 0.5$ , the  $\kappa$  and  $x$  are inverse proportion. When the  $x$  above 0.5, in this study with  $x=0.6$ , the  $\kappa$  is enlarge to near with the result of  $x=0.4$  and the shape of curve has changed. Next, that discuss to electric properties, in general, the materials'  $S$  and  $\rho$  are direct proportion. And the results are following this rule. In the end, it obtain the best  $ZT \sim 1.5$  at 300 K by  $x=0.45$  ingot in this study caused by the lowest electrical resistivity and proving the SPS process can effectively enhance the TE properties by the case of  $x=0.5$  and the first investigation. The carrier concentrations of  $x=0.45$  and  $x=0.5$  SPS are larger than  $10^{22}/\text{m}^3$  which have the  $ZT$  value large than 1.

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